



Laboratoire Matériaux
et Durabilité des
Constructions



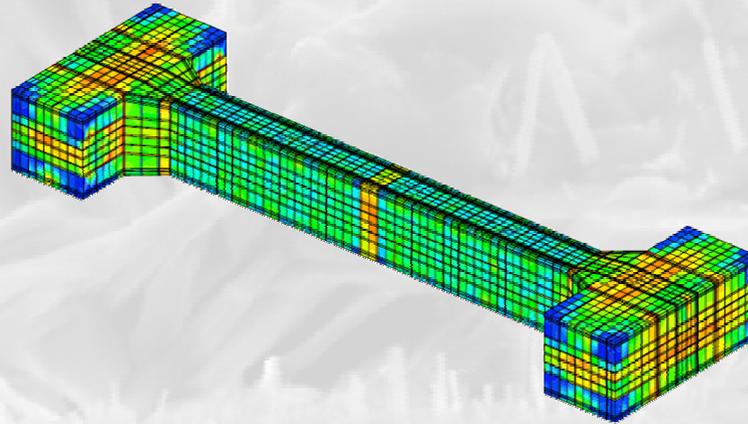
**Use of original percolation approach in
homogenization methods for the
prediction of concrete hydro-mechanical
behaviour at early age**



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Context : *CEOS.fr* and *Mefisto* French national projects

Task 2 : Concrete structure behaviour under THM loading



Previous studies and simulations

- ⇒ Need to improve the prediction of **mechanical properties** at very **early age**
- ⇒ Need to improve the modelling of **hydro-mechanical** behaviour (properties at **early age** and **hysteresis** phenomenon)

MEFISTO

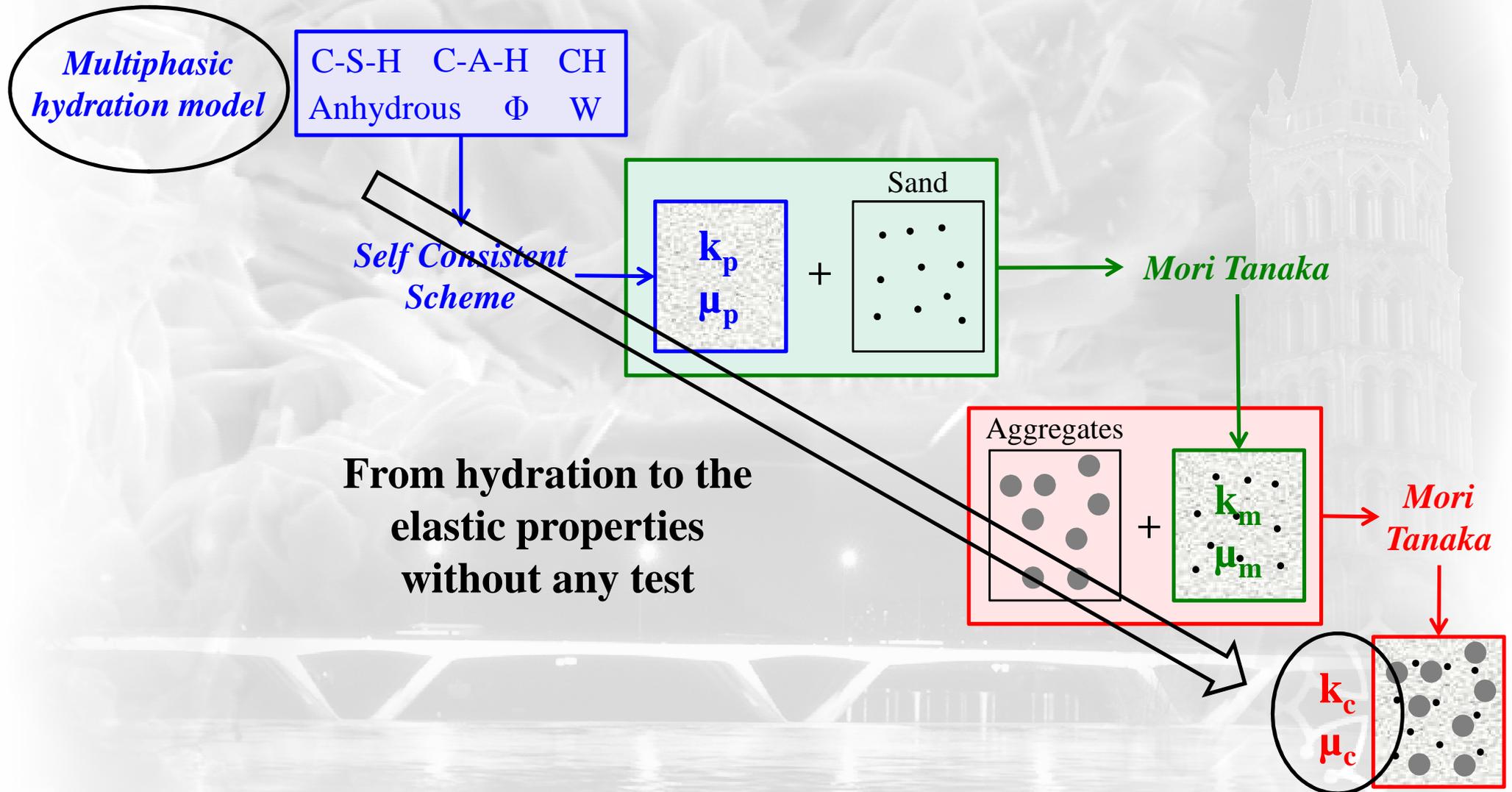
Use of **multi-scale approach** to predict **hydro-mechanical** properties according to **hydration** prediction

I – Principal of the multi-scale approach

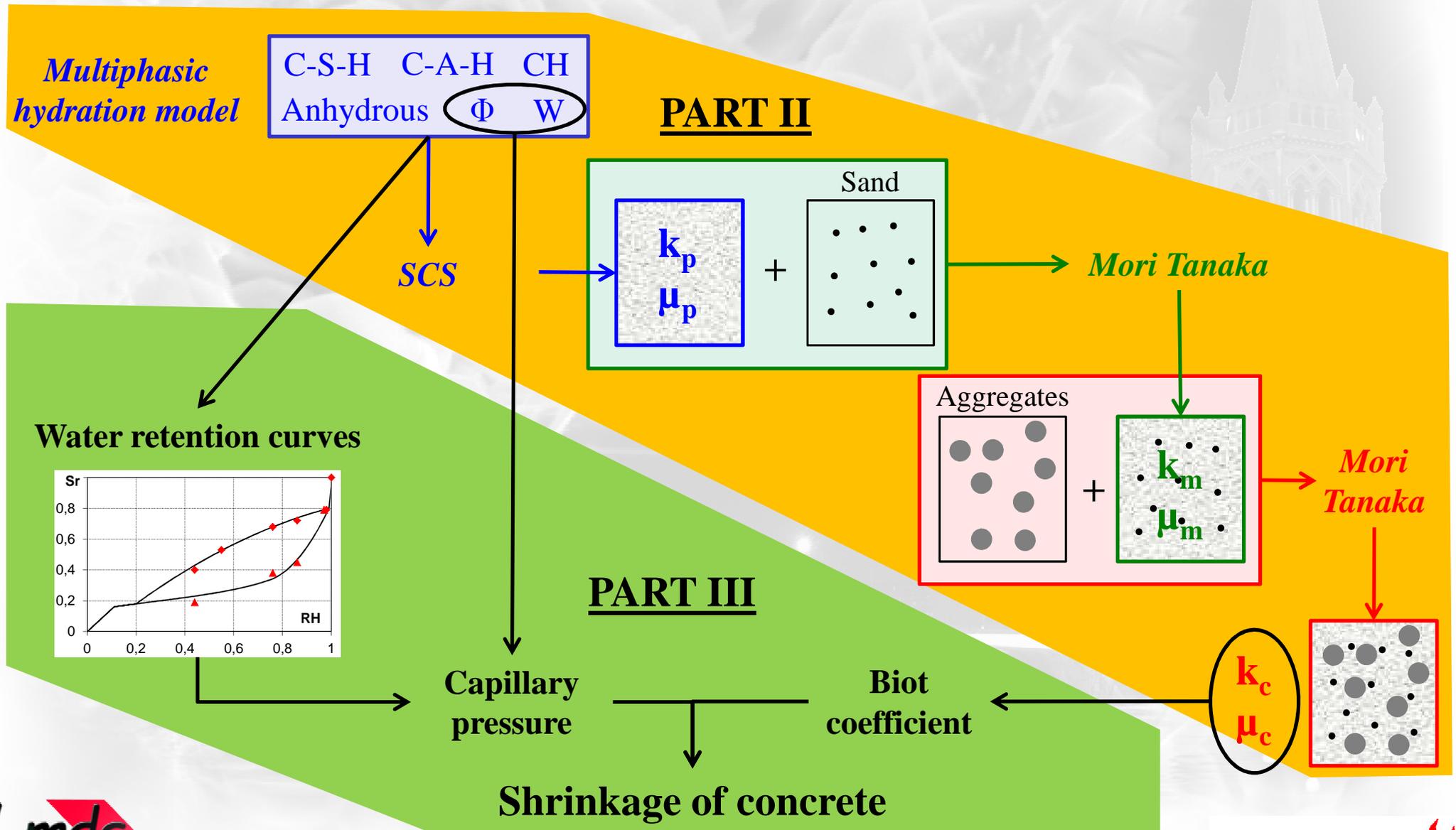
II – Prediction of elastic properties

III – Extension to the hydro-mechanical properties

Multi-scale homogenisation for the prediction of elastic properties



Extension to the prediction of shrinkage



I – Principal of the multi-scale approach

II – Prediction of elastic properties

III – Extension to the hydro-mechanical properties

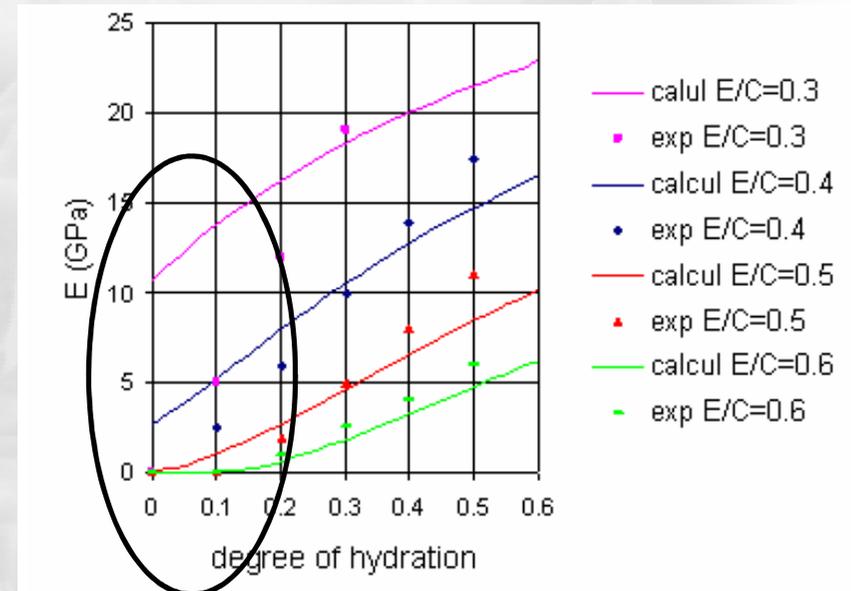
Paste level

Self consistent scheme

=> Percolation for solid fraction > 0.5

Overestimation of the mechanical percolation for low W/C ratios

(interface between solid phases able to transmit hydrostatic and shear stresses)



2 approaches in literature:

- Mechanical percolation algorithm ([Torrenti et al. 2005], [Smilauer et al. 2006])

=> *Unpercolated phases neglected even under hydrostatic stresses*

=> *Important computing time (incompatibility with structure calculation)*

- Shape of inclusions (C-S-H) [Sanahuja et al. 2007]

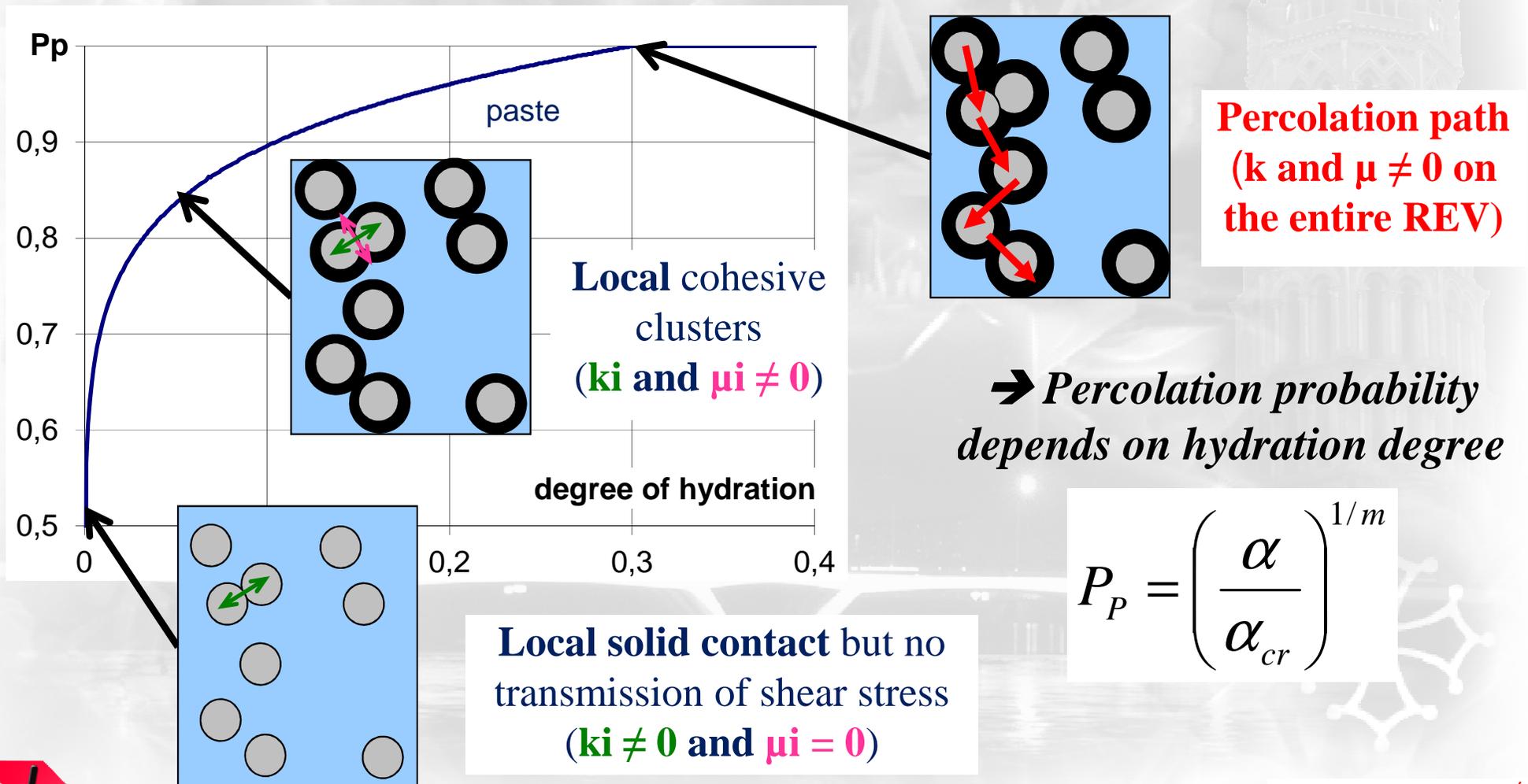
=> *Necessity to modify the shape to fit all W/C ratio results*

Approach proposed : Percolation probability to separate solid phases into cohesive or non-cohesive according to shear solicitations

Introduction of the percolation probability

Physical considerations

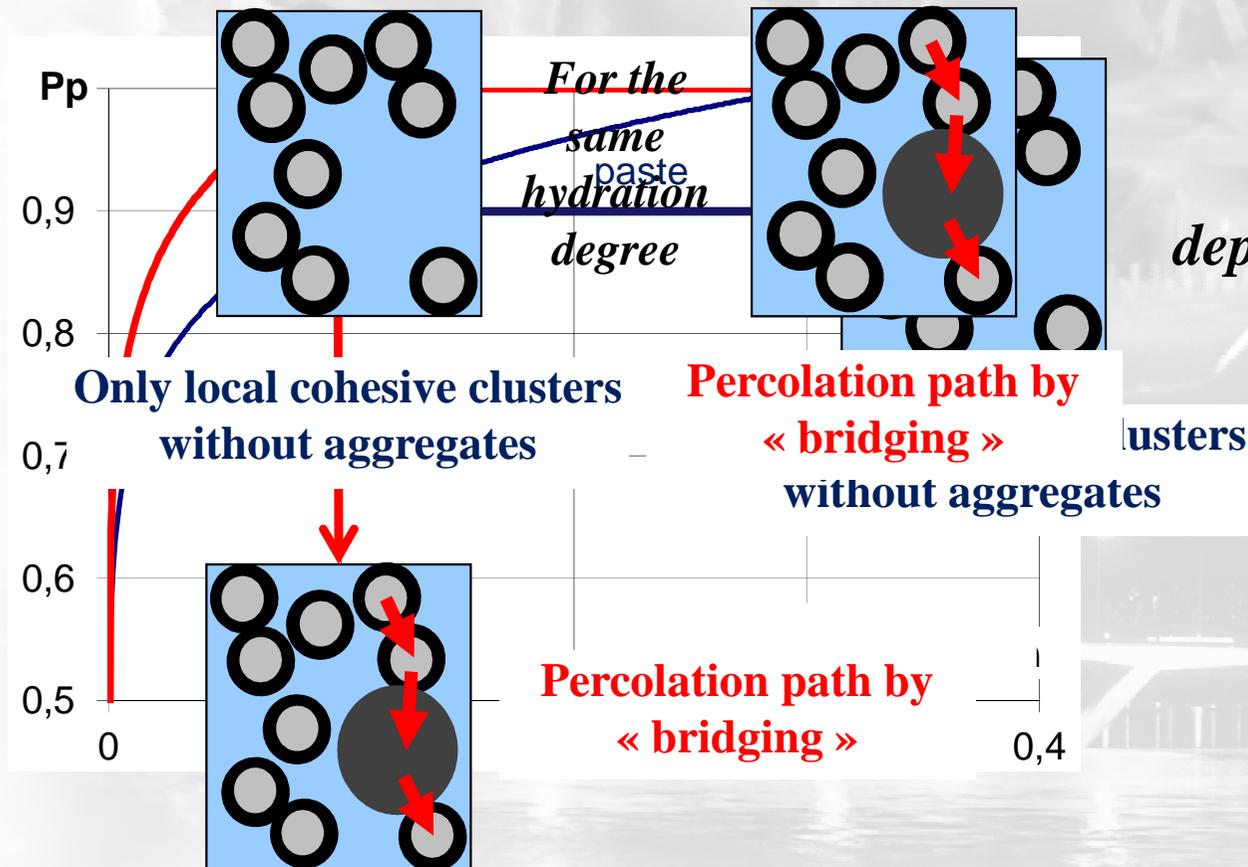
⇒ Mechanical percolation if solid phases linked with hydrates



Introduction of the percolation probability

Physical considerations

- ⇒ Mechanical percolation if solid phases linked with hydrates
- ⇒ “Bridge” effect of aggregates on percolation



→ Percolation probability depends also on aggregate content

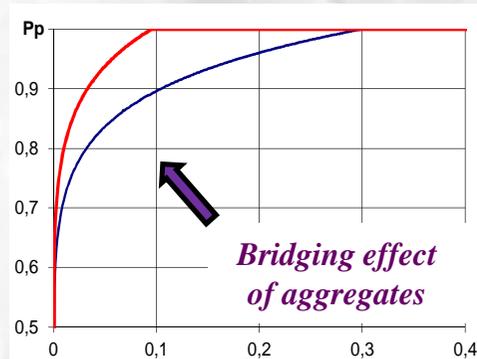
$$P_P = \left(\frac{\alpha}{\alpha_{cr}} \times \frac{1}{1 - \phi_g} \right)^{1/m}$$

Prediction of paste elastic properties

Multiphasic hydration model

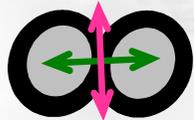


+ Percolation probability



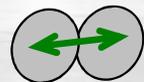
$$f_{i_{perc}} = P_P \cdot f_i$$

Percolated solid phases (k_i, μ_i)

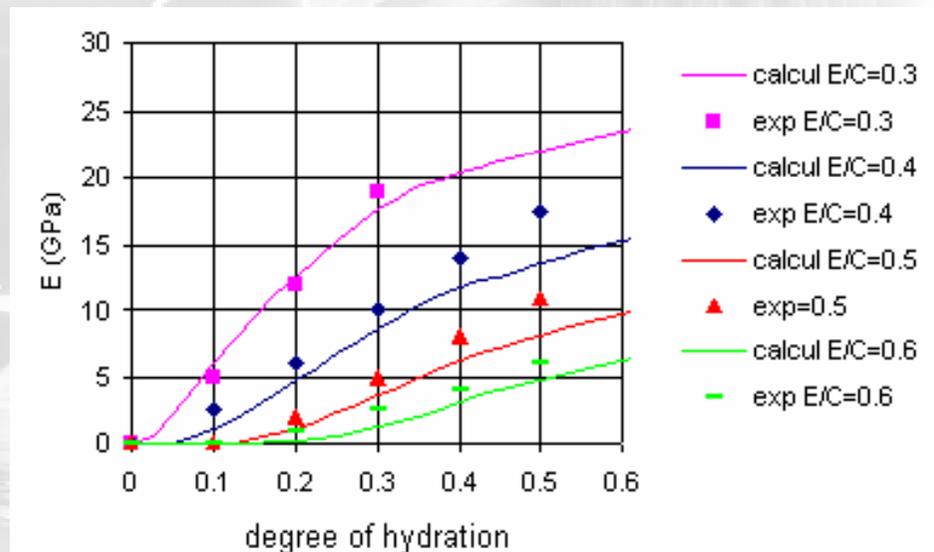
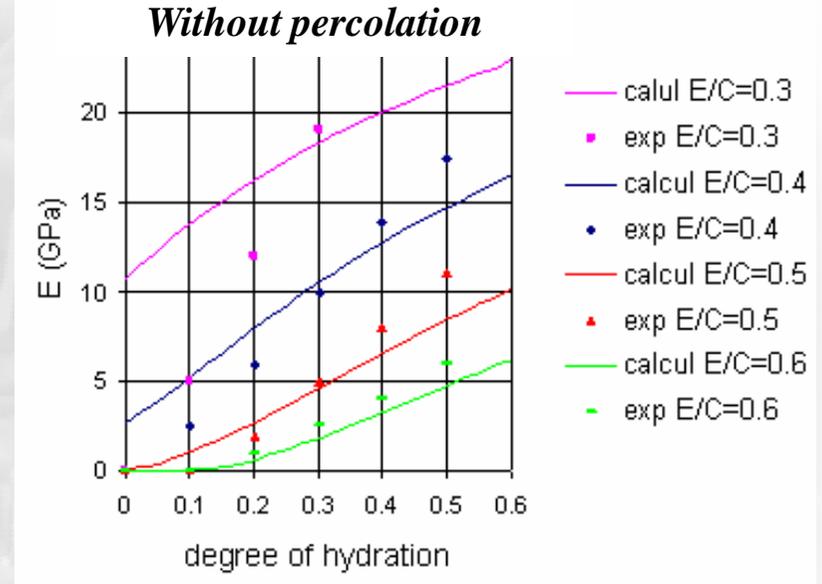


$$f_{i_{perc}} = (1 - P_P) \cdot f_i$$

Unpercolated solid phases ($k_i, \mu_i=0$)



SCS



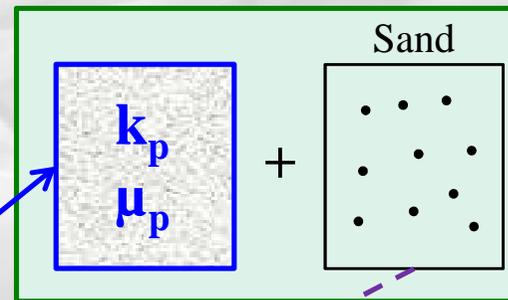
Conclusions on the multi-scale coupled method

- 3 levels with interactions of mortar and concrete levels on paste
- Original percolation function for realistic prediction of percolation development

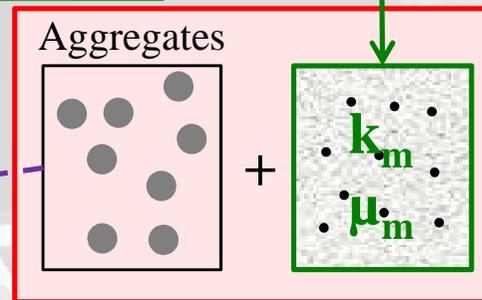
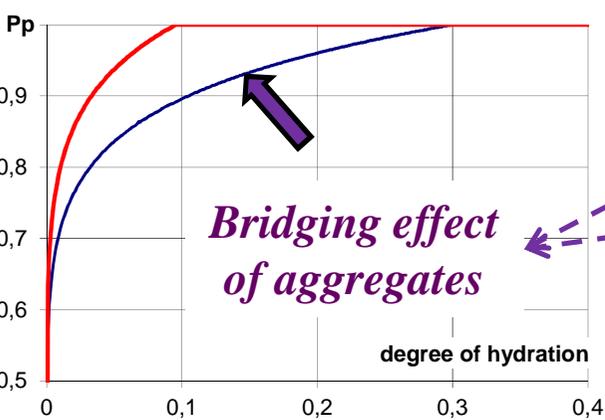
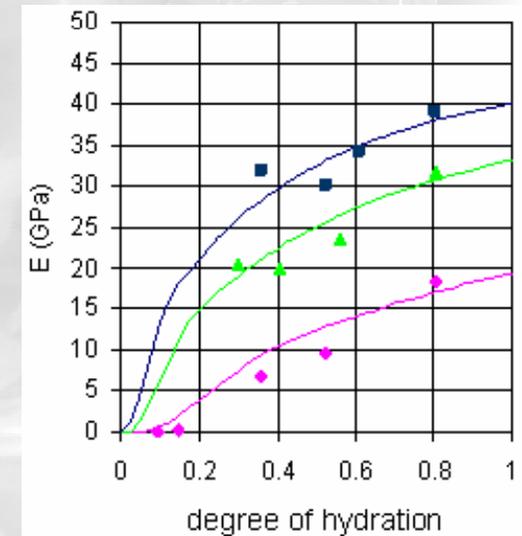
C-S-H C-A-H CH
Anhydrous Φ W

Multiphasic hydration model

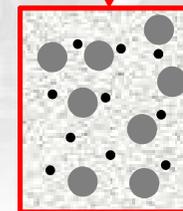
Self Consistent Scheme
+ Percolation probability



Mori Tanaka



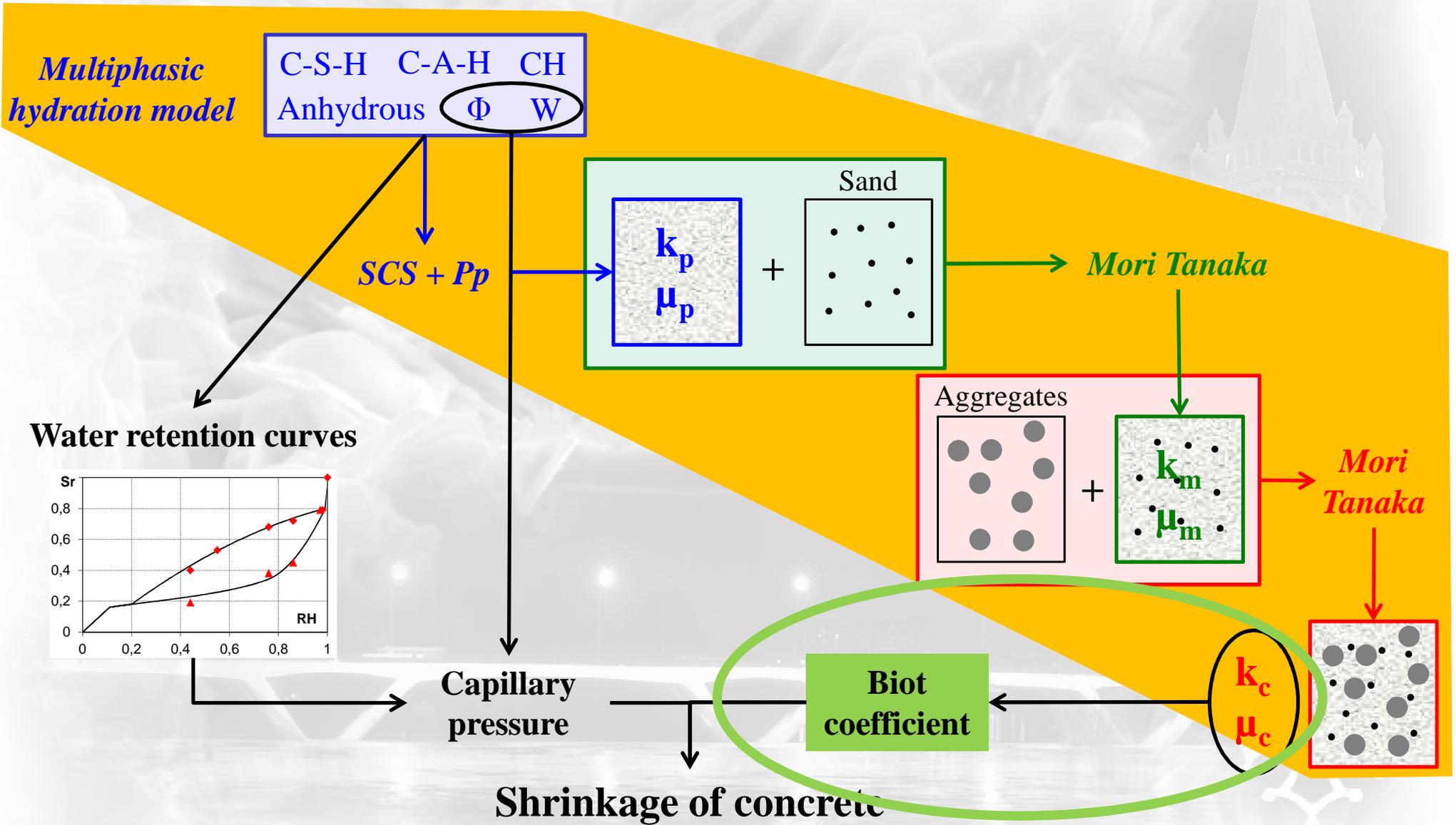
Mori Tanaka



I – Principal of the multi-scale approach

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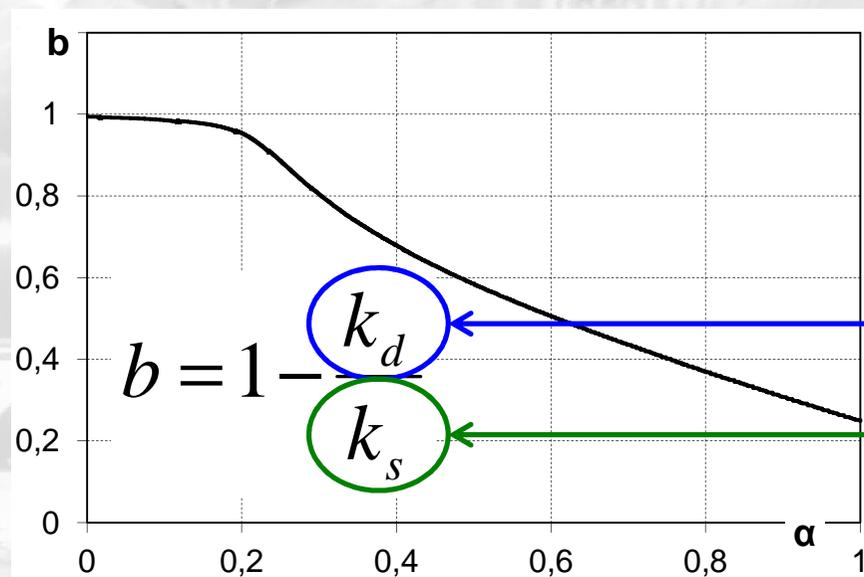
Assessment of Biot coefficient

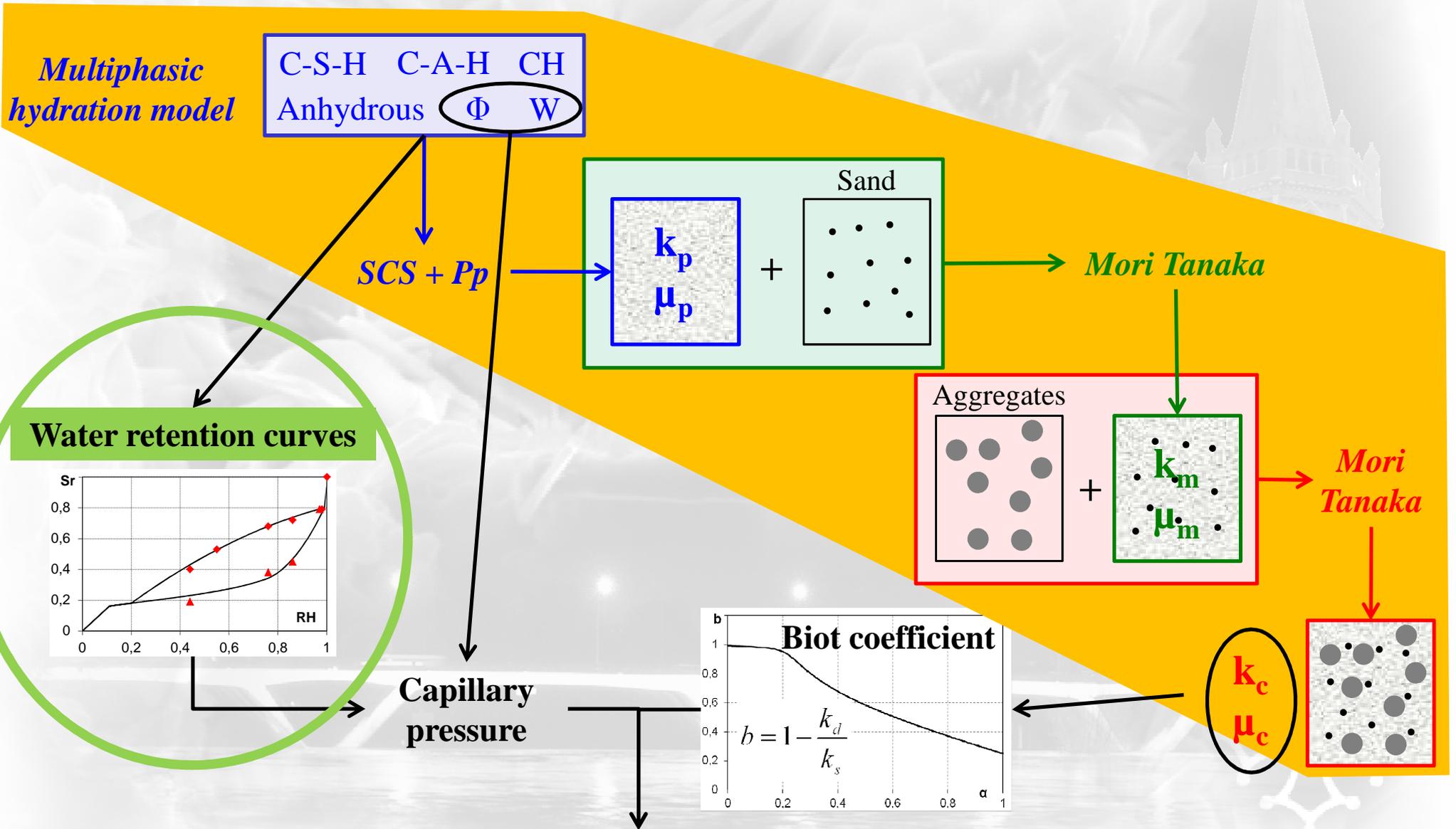
Application of multi-scale method on **drained material**

⇒ Compressibility of water taken equal to zero in the homogenisation of paste

Application of multi-scale method on solid **skeleton only**

⇒ Water and pore phases not taken into account in the homogenisation of paste

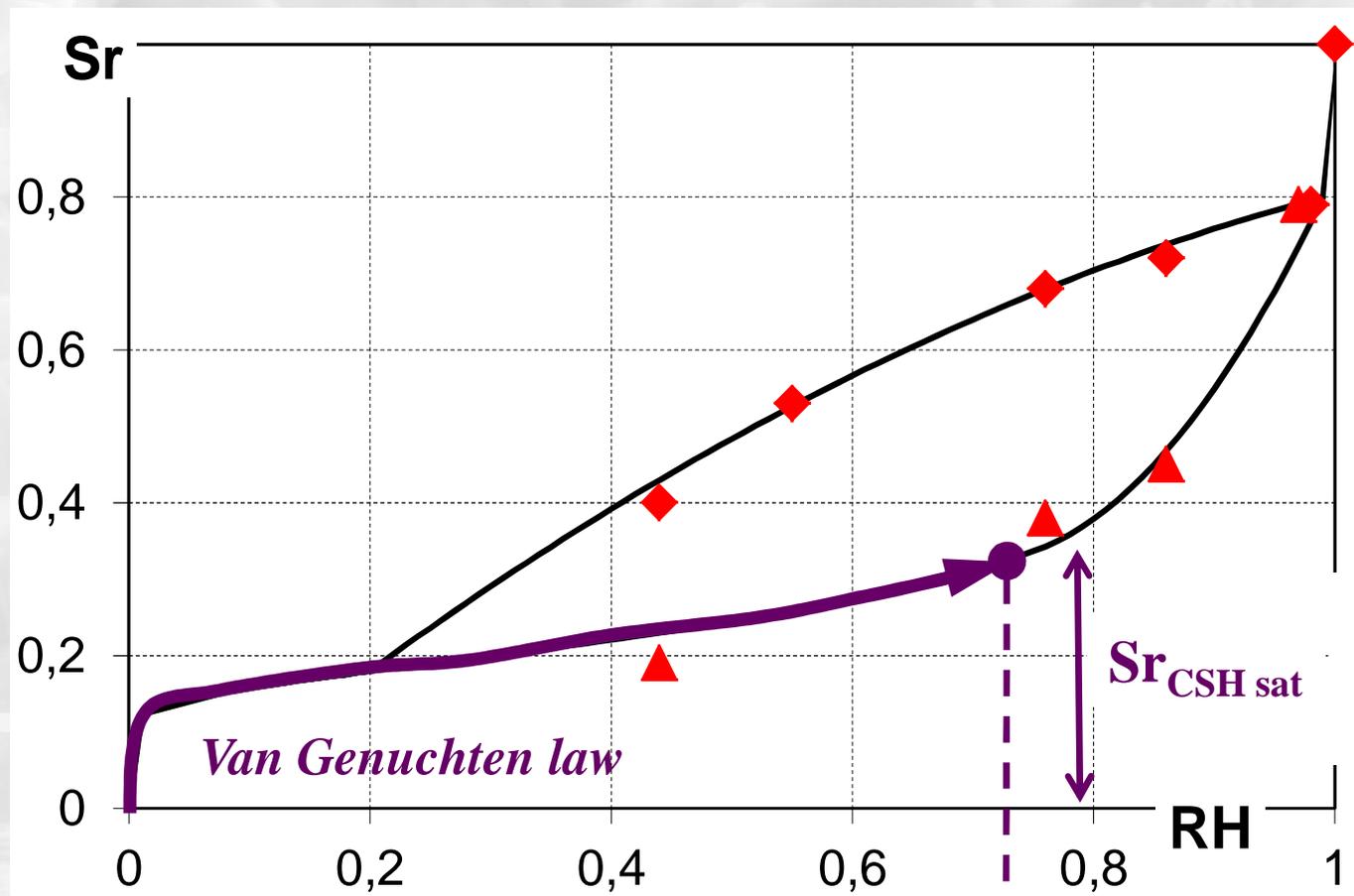




Modelling of water retention curves

Adsorption in cement based materials

⇒ For $RH < 75\%$: water in CSH → Van Genuchten adsorption law

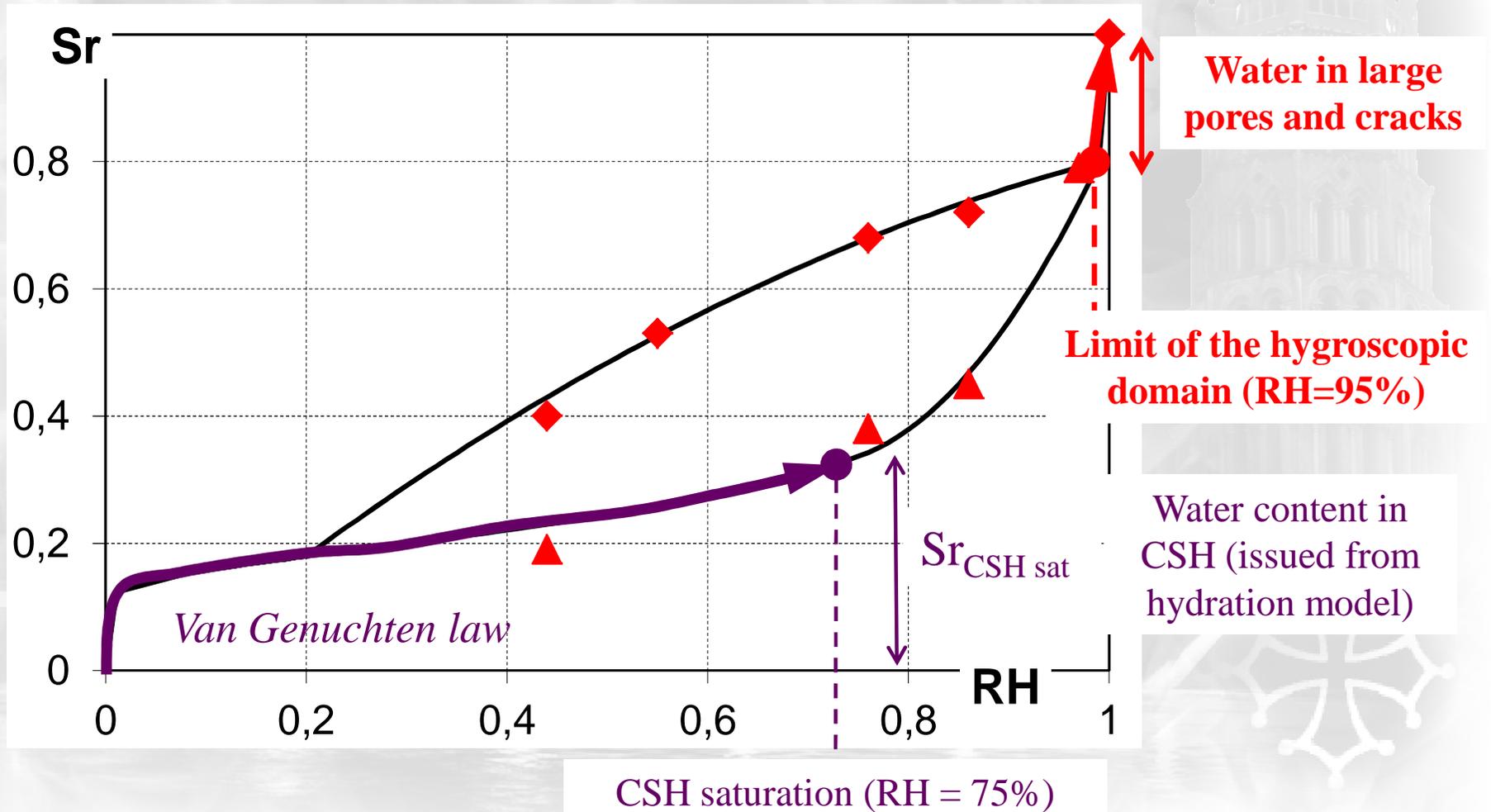


Water content in CSH (issued from hydration model)

Modelling of water retention curves

Adsorption in cement based materials

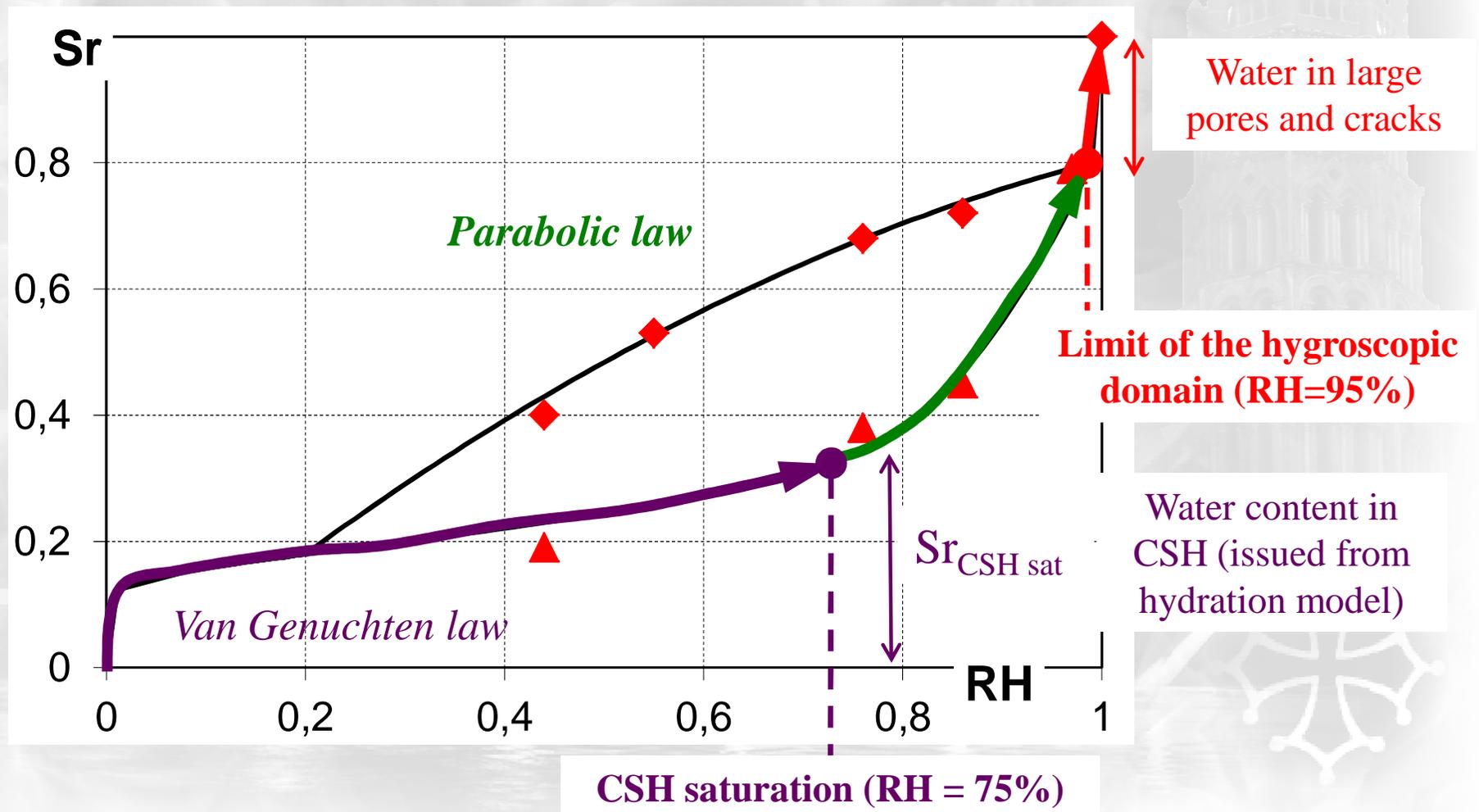
⇒ For $RH > 95\%$: over-hygroscopic domain (water in large pores and cracks)



Modelling of water retention curves

Adsorption in cement based materials

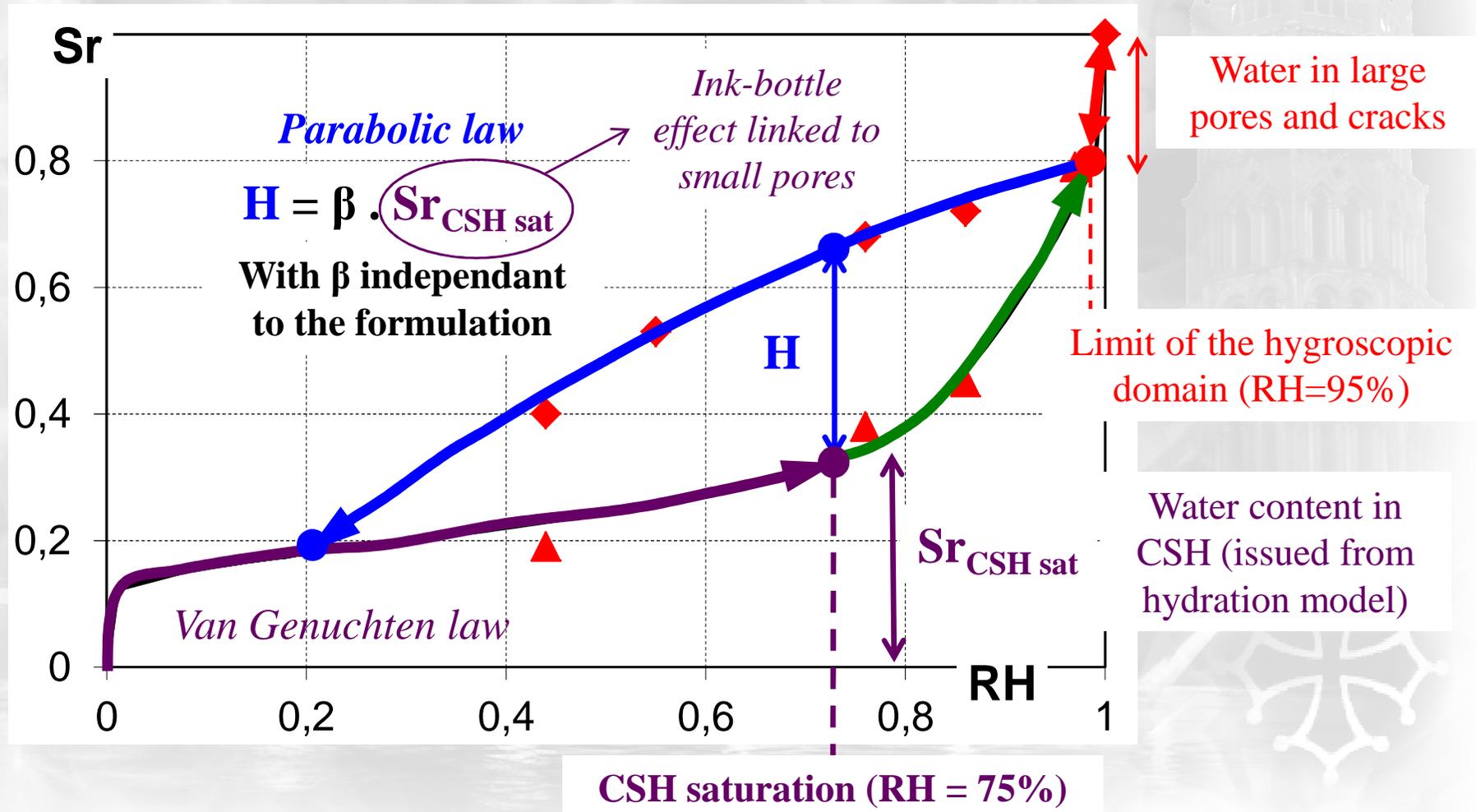
⇒ For $75\% > RH > 95\%$: Parabolic law to fit the 2 S_r values and gradient at 75%



Modelling of water retention curves

Desorption in cement based materials

⇒ **Hysteresis** phenomenon experimentally observed **between 20% and 95% RH**



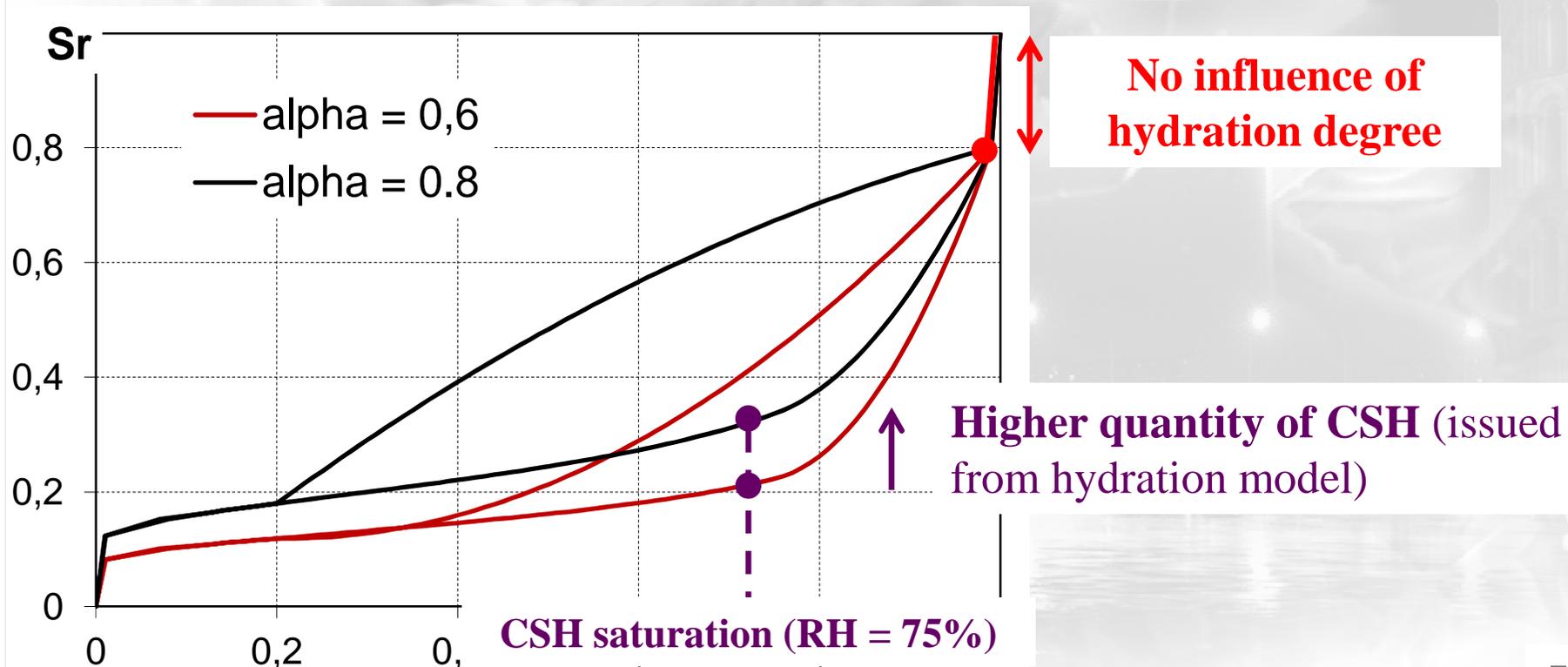
Modelling of water retention curves

Effect of hydration

Few results in literature: observation of more water content for a same relative humidity if hydration degree increases

⇒ More water content at CSH saturation (higher CSH quantity from hydration model)

⇒ No influence on the water in large pores and cracks

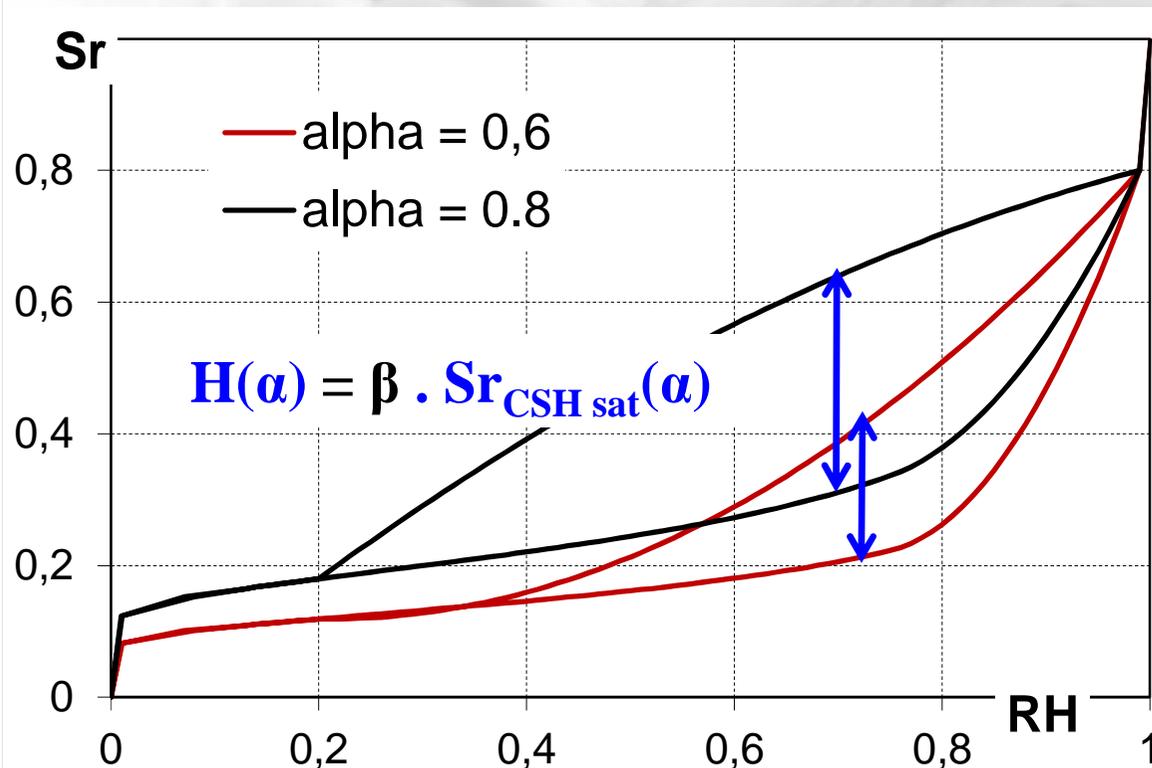


Modelling of water retention curves

Effect of hydration

Few results in literature: observation of more water content for a same relative humidity if hydration degree increase

- ⇒ More water content at CSH saturation (higher CSH quantity from hydration model)
- ⇒ No influence on the water in large pores and cracks
- ⇒ More hysteresis (but β not influenced by hydration degree)



Higher quantity of CSH predicted by hydration automatically leads to:

- higher water for a same RH
- higher hysteresis

→ *Water retention model seems to be adapted to different hydration degree **without modifying parameters***

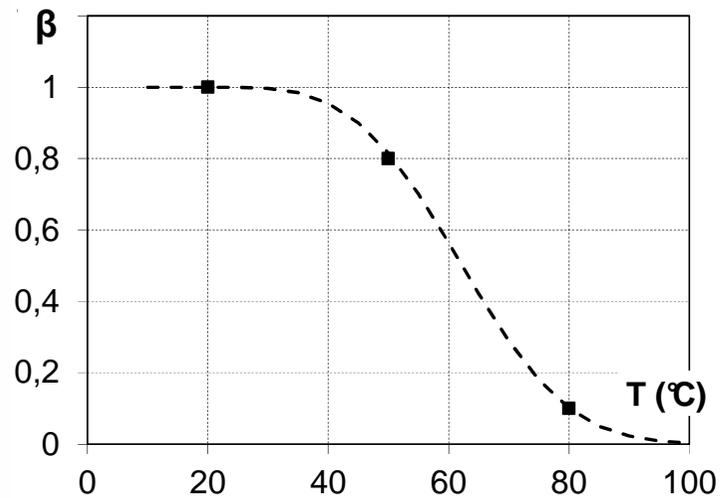
Modelling of water retention curves

Effect of temperature

Experimental results on the same concrete at 20, 50 and 80°C

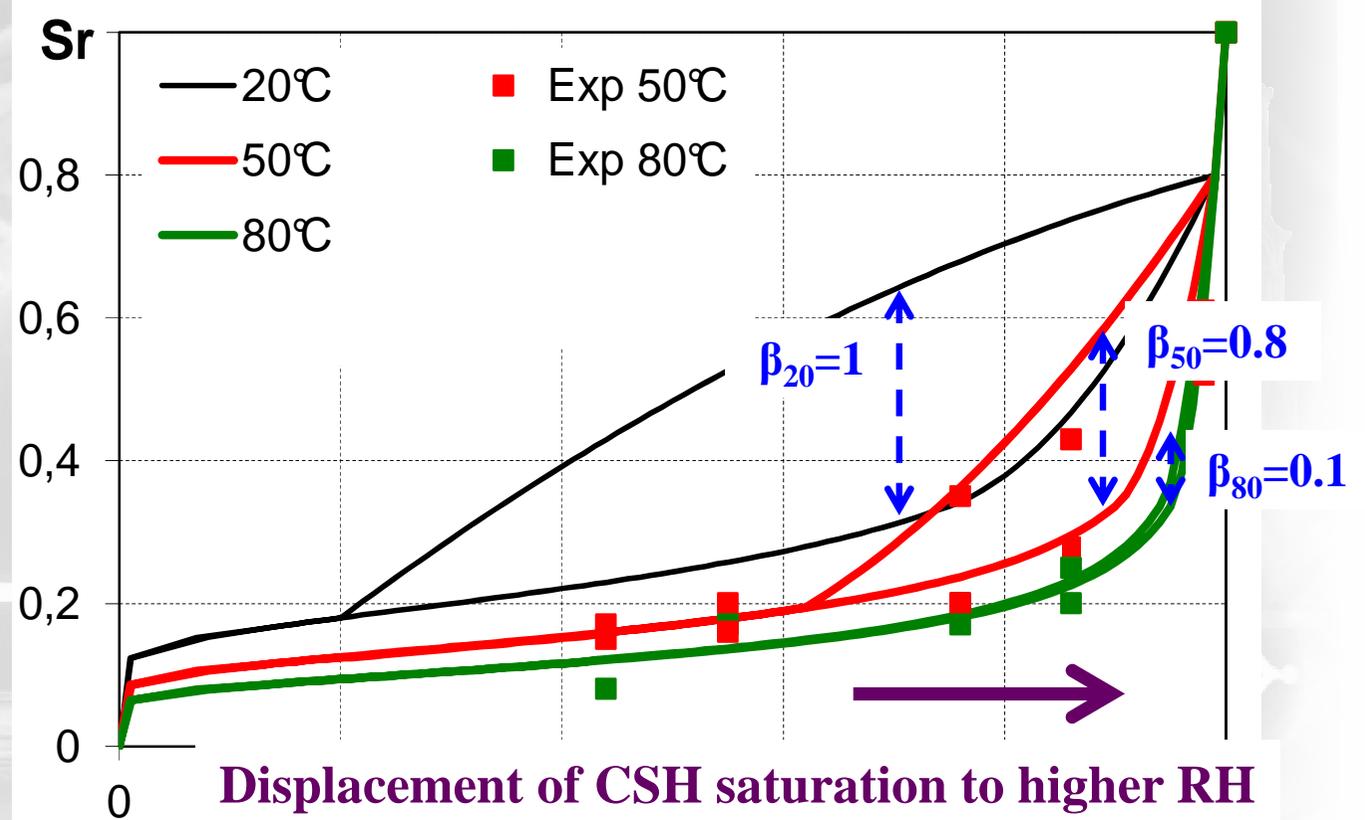
⇒ Less water content in hygroscopic domain

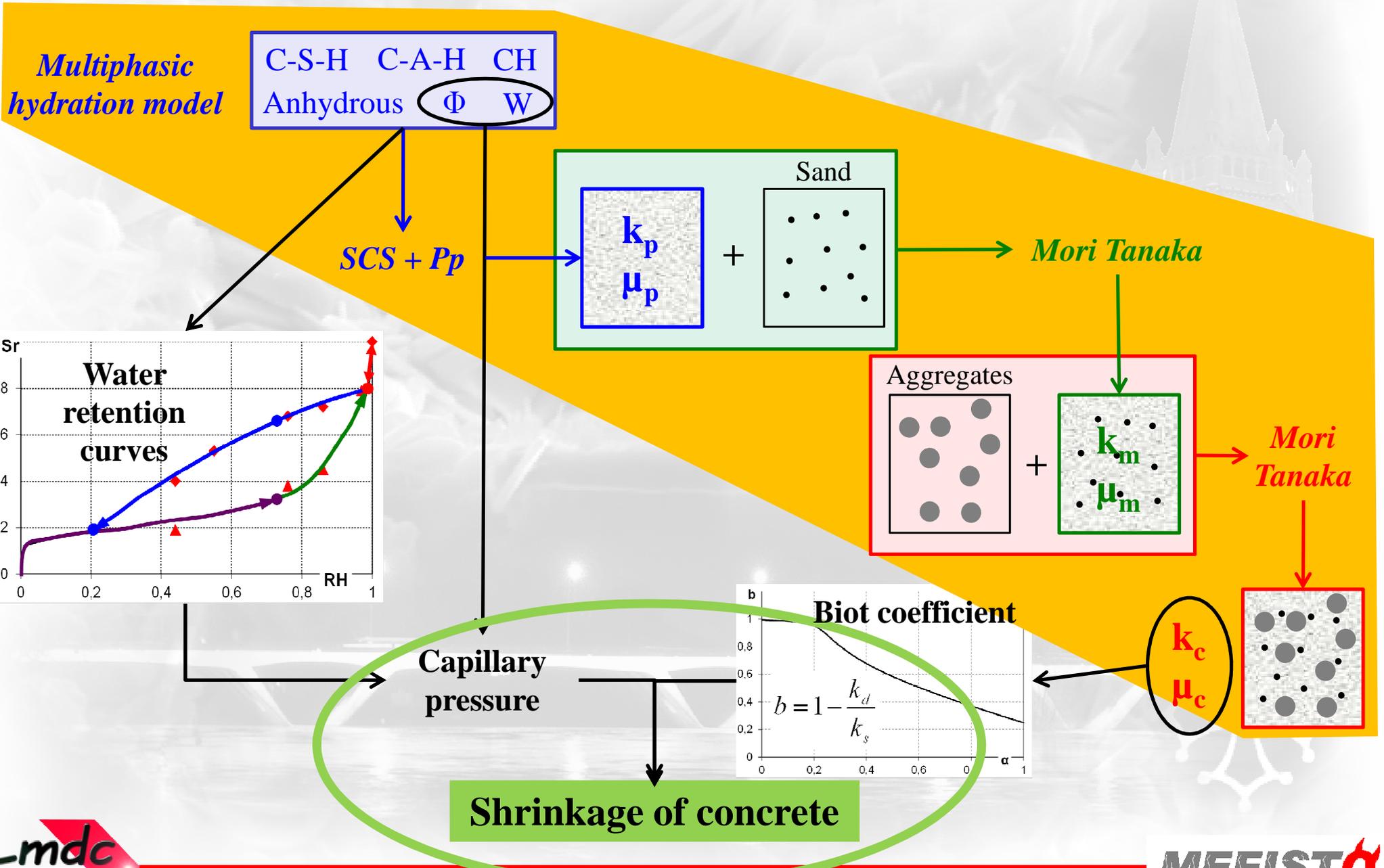
⇒ Less hysteresis (β decreases with temperature)



$$\beta = \exp\left(-\frac{1}{4} \times \left(\frac{3000}{T_{ref}} - \frac{3000}{T}\right)^4\right)$$

$$\beta = 1 \text{ for } T < 20^\circ\text{C}$$





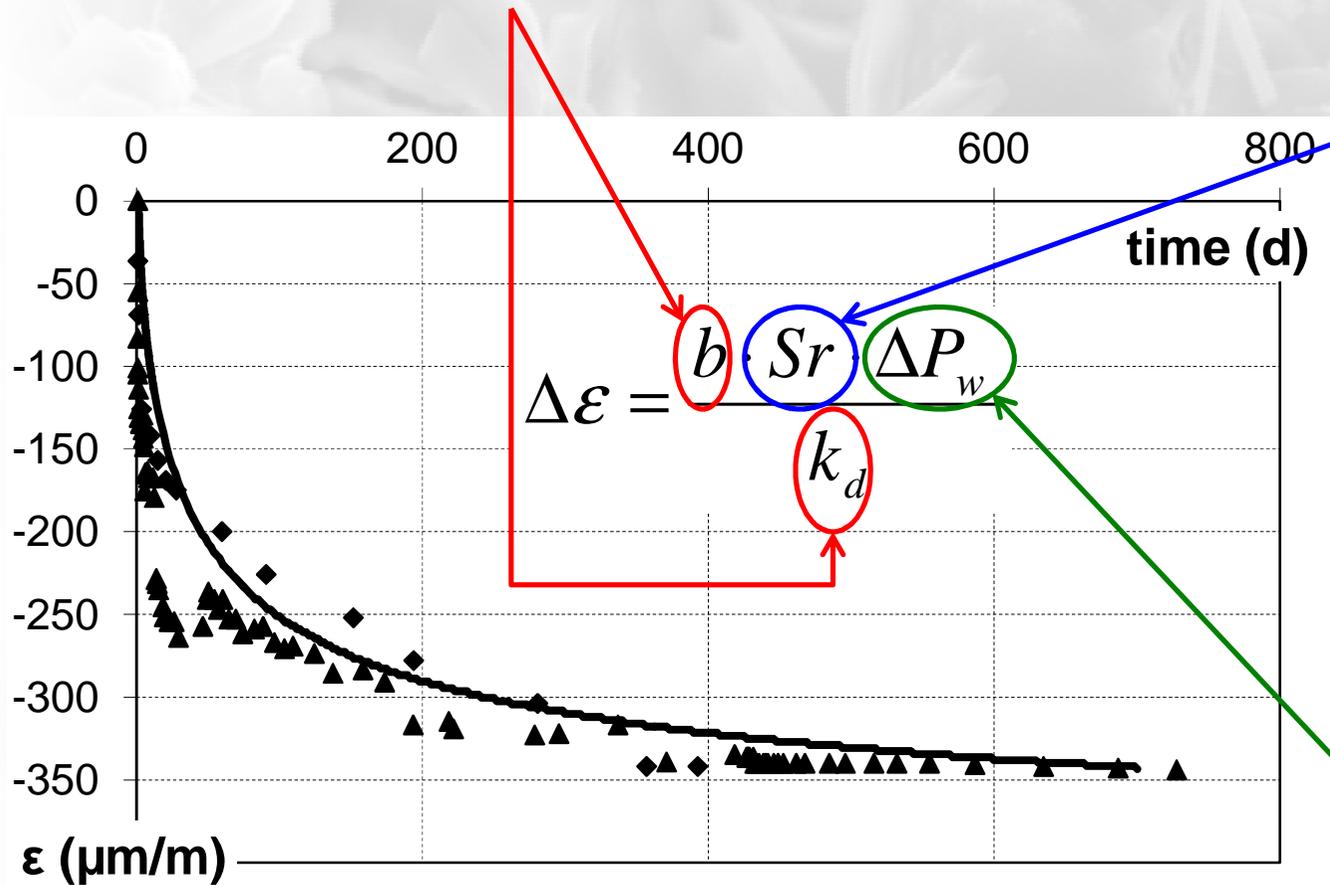
Prediction of autogenous shrinkage

Simplified shrinkage prediction: only elastic strain under water pressure

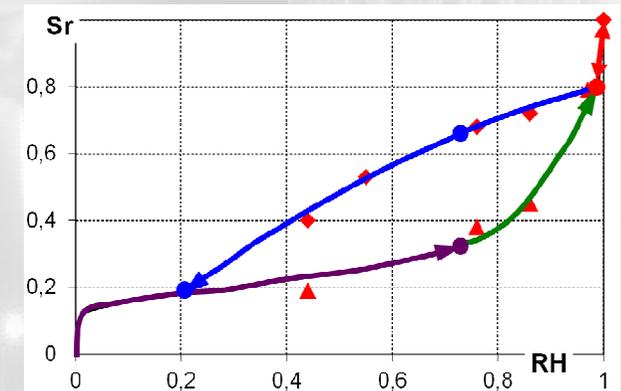
« Coupled level » homogenisation scheme with percolation

→ Coupling between creep and shrinkage: see presentation *Sellier et al.*

Multiphasic hydration model



Water retention curve model

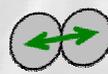


$$P_w = \frac{\rho_w RT}{M_w} \cdot \ln(RH)$$

Conclusions

• Original 3 coupled level method

→ Percolation probability to separate solids into cohesive (k_i, μ_i) and non-cohesive ($k_i, \mu_i = 0$)



→ Interaction between levels due to the “bridging effect” of aggregates

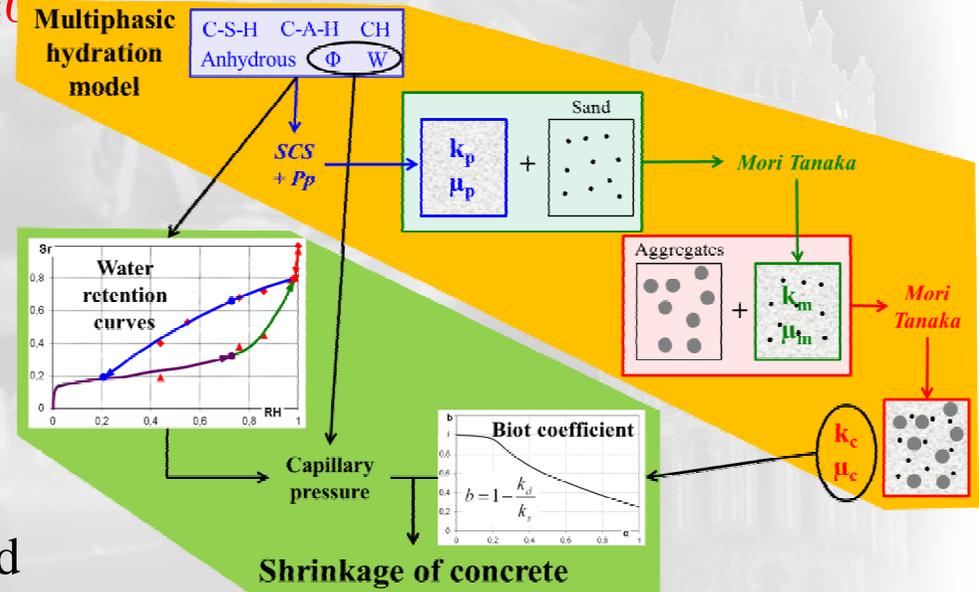
• Extension to the hygro-mechanical properties

→ Biot coefficient assessment by 2 applications of multi-scale method developed in Part. 1

→ Model of water retention curves based on hydration predictions (*effect of hydration and temperature included without re-fitting*)

Perspectives:

- More investigate the capability of hydro-mechanical properties model (water retention curves)
- Investigate the evolution of concrete thermal dilatation at early age





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