



# Numerical modelling of RC structure durability

- Multi-level concept and various coupled problems -

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# Outline



## 1 - *Introduction*

## 2 - Modelling of isothermal **Cl<sup>-</sup> transport** in concrete

**2.1** - Level 2: Multi-species transport model (sat. cond.)

**2.2** - Level 3: Advanced physical-chemical model (sat. cond.)

**2.3** - Level 4: Coupled moisture-ion transport model

## 3 - Modelling of **carbonation** of concrete

**3.1** - Level 2: Semi-analytical physical-chemical model - Probabilistic framework

**3.2** - Level 3: Numerical physical-chemical model

## 4 - Concluding remarks & further needed developments

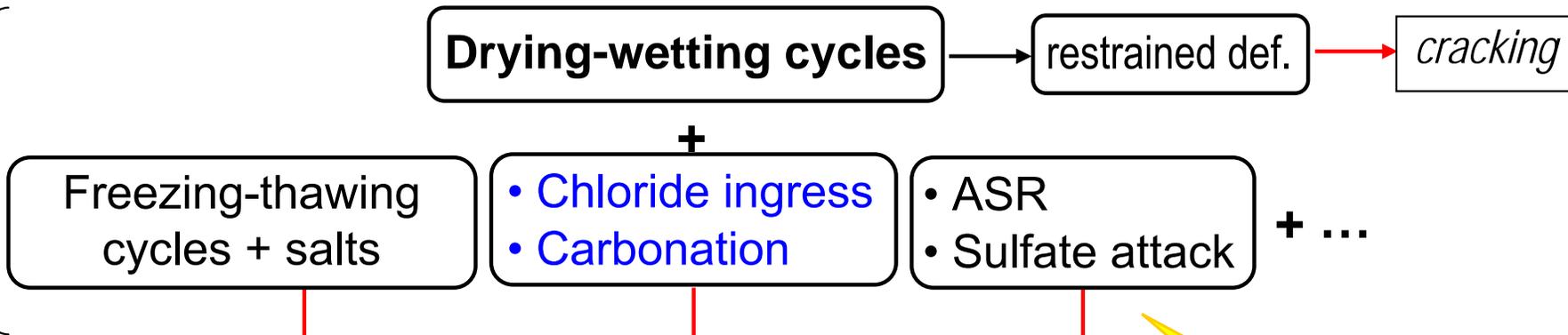




# 1 - A BASIC ISSUE FOR CONCRETE STRUCTURES ...

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coupled physical and chemical processes



**Microstructure**

**"Pure" transport properties + fluid-matrix interactions**

90% degradations

degradations

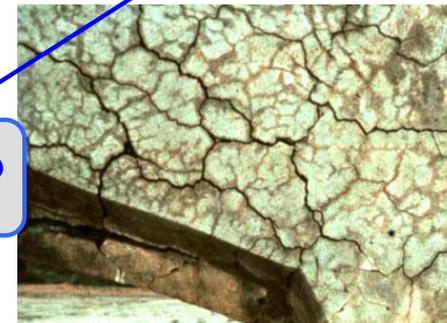
- Swelling
- Scaling

Reinforcement corrosion  
+ concrete degradations

Swelling + cracking + ...



**Durability ?**



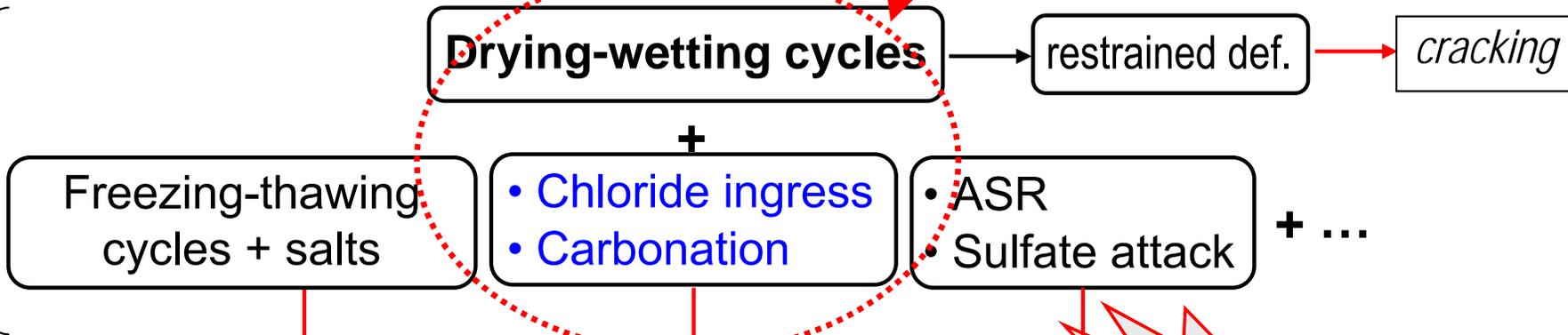
fundamental aspect of sustainability





# 1 - A BASIC ISSUE FOR CONCRETE STRUCTURES ...

coupled  
physical and  
chemical  
processes



**Microstructure**

**"Pure" transport properties + fluid-matrix interactions**

**Durability indicators**

degradations

• Swelling  
• Scaling

Reinforcement corrosion  
+ concrete degradations

Swelling + cracking + ...

**Durability ?**

**Monitoring parameters**

**Cost ?**





# 1 - PURPOSES OF NUMERICAL MODELLING IN THE FIELD OF DURABILITY

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## \* Better understanding, description and implementation of phenomena

- multi-species & multi-phase transport, realistic field conditions (wetting-drying cycles, complex BCs...), coupling between ageing and degradation, physical-chemical-(mechanical) coupling, multi-scale problems

## \* Accurate prediction of ingress of aggressive species and of SL

- SL prediction at the design stage, prediction of future evolution of existing structures, selection of appropriate security margins (probabilistic framework)
  - (very) long-term durability assessment (special structures)
  - help diagnosis and optimise monitoring of RC structures

## \* Concrete mix-design or concrete cover design for a predefined SL

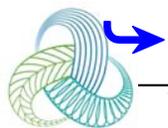
- multi-criteria optimisation of the composition of the material, probabilistic-based selection of optimum concrete cover



- improve the link between **mix-design** & structural **lifetime**
- enhance the use of "green" concretes + ensure **durability**



## \* Assessment of input data of models



- transport properties & CI- binding isotherms by num. inverse analysis

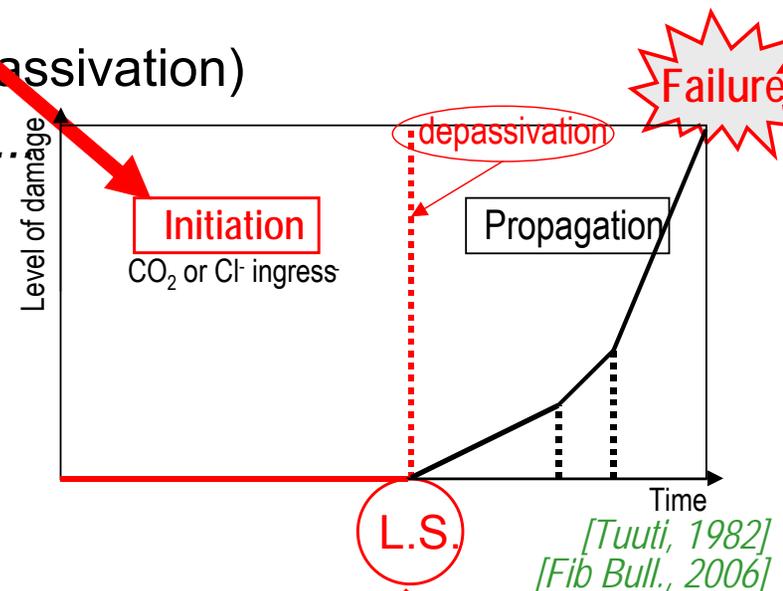
# 1 - NUMERICAL PREDICTIVE MODELS

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- Main features (protection against carbonation- or Cl<sup>-</sup>-induced corrosion) •

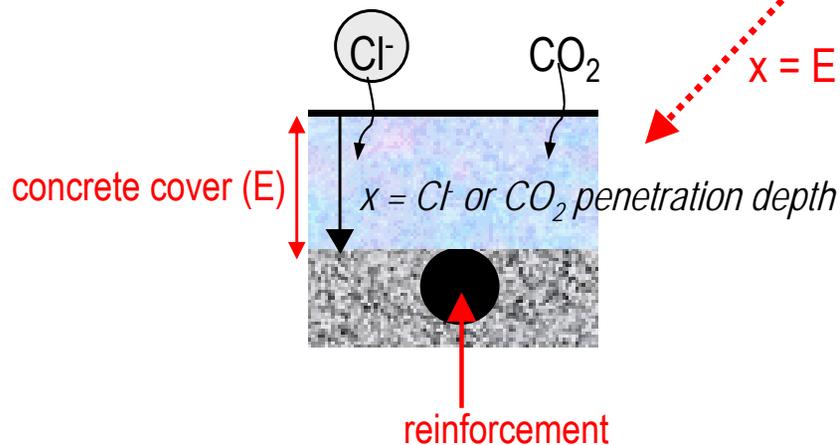
\* **Assumption:** restriction to the initiation period  
(limit state (L.S.) = reinforcement depassivation)

↳ **conservative, material approach, ...**



End of life: the aggressive species penetration front reaches the 1<sup>st</sup> layer of rebars

↳ uncracked concrete



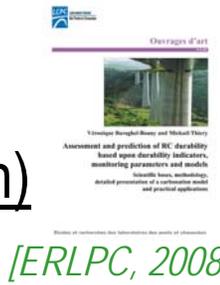
\* **Other approaches:** integration of part of propagation period (corrosion, cracking)

[Andrade, 2008], [Alexander, Microdurability, 2012], [Michel et al. Microdurability, 2012]

# 1 - NUMERICAL PREDICTIVE MODELS



- Main features (protection against carbonation- or Cl-induced corrosion)



[ERLPC, 2008]

\* **Assumption:** restriction to the initiation period

- physically and chemically based
- deterministic or probabilistic framework
- **durability indicators** (transport prop., ...) → main input data
- **monitoring parameters** (kinetics & conc. profiles) → output data

➔ **set of numerical models** (macroscale, isoth. cond., uncracked concrete) with different levels of sophistication for each process

➔ *but the high d° of complexity may need in some cases to include analytical descriptions or coupling with analytical tools*

- Bil code (C++)
- 1-D Finite volume method (spatial discretization)
- Euler implicit scheme (time discretization)
- standard Newton algorithm

from simple tools to advanced physical-chemical models

e.g. - Cl- ingress  
- Carbonation



➔ **Multi-level platform**

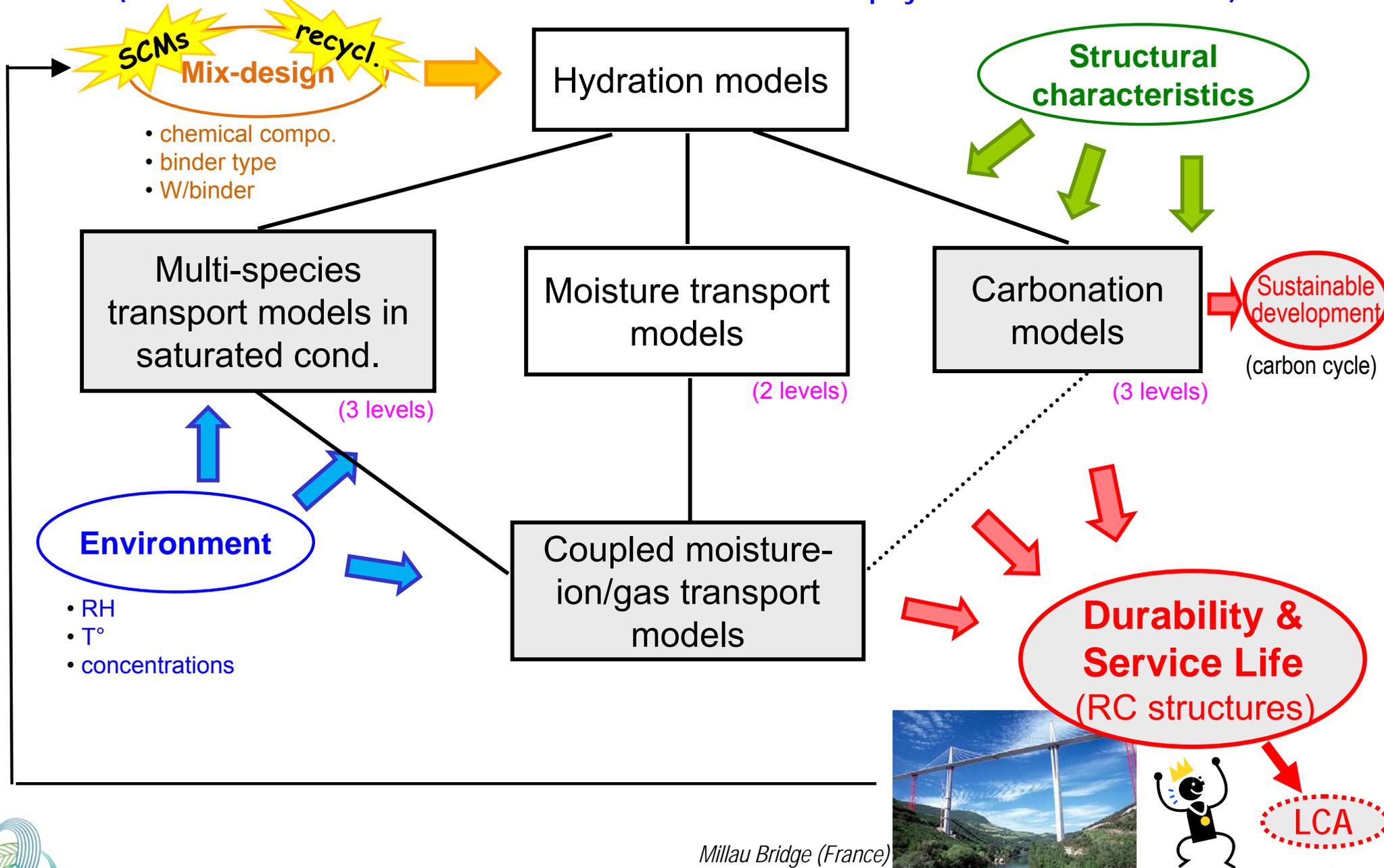


# 1 - MULTI-LEVEL NUM. MODELLING PLATFORM FOR DURABILITY ASSESSMENT

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- Protection against carbo.- or Cl-induced corrosion ●

(uncracked material & macro-scale - Isoth. cond. - 1-D physical-chemical models)



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2 - ***Modelling of isothermal Cl<sup>-</sup> transport in concrete***

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## 2 - MULTI-LEVEL CONCEPT APPLIED TO MODELLING OF Cl<sup>-</sup> TRANSPORT IN CONCRETE

\*\*\*\*\*

[Baroghel-Bouny et al., CCC, 2009]

- Multi-level platform (1-D physical numerical model) ●

➔ **4 levels of sophistication**

- Level 1 - Chloride diffusion model (sat. cond.)

- Cl<sup>-</sup> diffusion (in diluted solution) → **Fick's 1<sup>st</sup> law**
- (global) Cl<sup>-</sup> binding → **Freundlich's** non-linear isotherm
- empirical law  $D_{Cl^-} = f(c_{Cl^-})$

[Andrade, CCR, 1993]  
[Masi et al., CCR, 1997]  
[Samson et al., 1999]  
[Truc et al., RILEM, 2000]

- Level 2 - Multi-species transport model (sat. cond.)

- **4 ions + electrical interactions** between ions → **Nernst-Planck/Poisson eq.**
- equil. Cl<sup>-</sup> binding → **various options** ➔ *analytical formula*  $s_{Cl^-} = s_{Cl^-}(c_{Cl^-})$

Multi-species approach

- Level 3 - Advanced physical-chemical model (sat. cond.)

- **6 to 8 ions + 3 to 8 solid compounds**
- Cl<sup>-</sup> binding → **physical adsorption** onto C-S-H + **Friedel's salt formation** by (instant.) chemical reactions (dissol./precip.)
- **microstructural** (and transport property) **changes** (induced by *Friedel's* salt precipitation, Ca(OH)<sub>2</sub> dissolution, ...)

- Level 4 - Coupled moisture-ion transport model

- ↳ contribution of **advection** to the overall ionic transport
- ↳ multi-species transport model (**level 2**) extended to **non-sat. cond.**

Increasing level of sophistication



# 2 - MULTI-LEVEL CONCEPT APPLIED TO MODELLING OF $\text{Cl}^-$ TRANSPORT IN CONCRETE

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- empirical law  $D_{\text{Cl}^-} = f(c_{\text{Cl}^-})$

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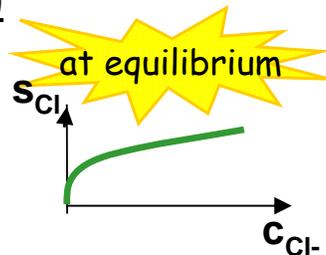
**Multi-species approach**

Increasing level of sophistication

Global description (*Freundlich's formula*)

$$s_{\text{Cl}^-} = \mu c_{\text{Cl}^-}^\gamma$$

*Freundlich's parameters*



Ion exchange theory description

$$s_{\text{Cl}^-} = \underbrace{\delta_3 N_{(\text{C}_3\text{A})\text{eq.}}}_{\text{chemical}} + \underbrace{N_{\text{C-S-H}}}_{\text{physical}} \frac{\alpha'' c_{\text{Cl}^-}}{c_{\text{OH}^-} + \beta'' c_{\text{Cl}^-}}$$

fixed parameters

pH effect

$s_{\text{Cl}^-}$  : total amount of bound  $\text{Cl}^-$  (mol / m<sup>3</sup> of mat.)  
 $c_{\text{Cl}^-}$  :  $\text{Cl}^-$  conc. of the pore sol. (mol / m<sup>3</sup> of sol.)

[Baroghel-Bouny et al., CCR, 2012]

# 2.1 - MULTI-SPECIES TRANSPORT MODEL (SAT. COND.)

\*\*\*\*\*

[Nguyen et al., C&C, 2006]

Level 2

- Transport and mass balance equations

\* Ions: Cl<sup>-</sup>, Na<sup>+</sup>, K<sup>+</sup>, OH<sup>-</sup>

\* Transport of each ion → Nernst-Planck equation

Poisson's equation

$$\text{div}(\text{grad } \Psi) + \frac{F}{\epsilon} (\sum c_i z_i) = 0$$

dielectric constant

[Samson et al., 1999 → 2003]

Flux ( $\text{mol} \cdot \text{m}^{-2} \cdot \text{s}^{-1}$ )  
( $i = \text{Cl}^-, \text{Na}^+, \text{K}^+, \text{OH}^-$ )

$$J_i = -D_i \text{grad} c_i + c_i \text{grad}(\ln \gamma_i) + \frac{z_i F}{RT} c_i \text{grad} \Psi$$

(constant) **effective ionic diffusion coef. of the saturated mat.** ( $\text{m}^2 \cdot \text{s}^{-1}$ )      chemical activity coef. (-)      **local elec. potential** (V)  
(ion-ion interactions)

$c_i$ : (free) conc. in ion  $i$  of the pore solution ( $\text{mol} / \text{m}^3$  of sol.)

$z_i$ : valence number of ion  $i$  (-)

$T$ : absolute temperature (K)

$R$ : ideal gas constant ( $8.3143 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$ )

$F$ : Faraday constant ( $9.64846 \cdot 10^4 \text{ C} \cdot \text{mol}^{-1}$ )

$$\gamma_i = 1$$

[Truc et al., RILEM, 2000]

[Marchand et al., M&S, 2002]

[Nguyen et al., C&C, 2006]



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\* Ions: Cl<sup>-</sup>, Na<sup>+</sup>, K<sup>+</sup>, OH<sup>-</sup>

\* Transport of each ion → Nernst-Planck equation

Flux (mol.m<sup>-2</sup>.s<sup>-1</sup>) (i = Cl<sup>-</sup>, Na<sup>+</sup>, K<sup>+</sup>, OH<sup>-</sup>) →

$$J_i = -D_i \text{grad} c_i + c_i \text{grad}(\ln \gamma_i) + \frac{z_i F}{RT} c_i \text{grad} \Psi$$

(constant) **effective ionic diffusion coef. of the saturated mat.** (m<sup>2</sup>.s<sup>-1</sup>)    chemical activity coef. (-)    **local elec. potential** (V) (ion-ion interactions)

\* Mass balance equation for each element (i = Cl, Na, K, O, H)

$$\frac{\partial n_i}{\partial t} + \text{div} J_i = 0$$

total content (mol / m<sup>3</sup> of mat.) (e.g. n<sub>Cl</sub> = φ c<sub>Cl<sup>-</sup></sub> + s<sub>Cl</sub>)

total amount of bound Cl<sup>-</sup> (mol / m<sup>3</sup> of mat.)

(free) Cl<sup>-</sup> conc. of the pore sol. (mol / m<sup>3</sup> of sol.)

**porosity** (-) (constant)

e.g. **Freundlich's formula**: s<sub>Cl</sub> = μ c<sub>Cl<sup>-</sup></sub><sup>γ</sup>

**s<sub>Cl</sub> = s<sub>Cl</sub>(c<sub>Cl<sup>-</sup></sub>)** → **Cl<sup>-</sup> binding isotherm**

and s<sub>i</sub>=0 for j≠Cl

at equilibrium



# 2.1 - MULTI-SPECIES TRANSPORT MODEL (SAT. COND.)

\*\*\*\*\*

- Input data required for the model •

Level 2

few inputs

Durability indicators

assumed independent of age and depth

(non-reactive porous solid)

$\phi$	Porosity accessible to water ( $m^3 \cdot m^{-3}$ )
$D_{Cl^-}$	Effective $Cl^-$ diff. coefficient ( $m^2 \cdot s^{-1}$ )
$s_{Cl} = s_{Cl}(c_{Cl^-})$	$Cl^-$ binding isotherm (at equilibrium)
I.C. (pore sol.) $\{ c_{Na^+}^0, c_{K^+}^0, c_{OH^-}^0 \}$	Initial chemical compo. of the pore solution $(C_{Cl^-}^0 = 0)$

exp. or anal. formula or num. inverse analysis

+ B.C.:  $T^\circ$  (constant), ionic conc. of the contact solution, ...

$c_{Na^+}^0, c_{K^+}^0$ : mix-compo. + cement chem. compo. + initial alkali binding  
 [Taylor, ACR, 1987] + hydration model + sat. sol. compo.  
 $c_{OH^-}^0 = c_{Na^+}^0 + c_{K^+}^0$

$$\frac{D_i}{D_i^0} = \frac{D_{Cl^-}}{D_{Cl^-}^0} (= \tau \cdot \phi) = \frac{1}{F} \quad (i \neq Cl^-)$$

[Samson, 1999]

at infinite dilution

[Mounanga et al., CCR, 2004]  
 [Nguyen, PhD thesis, 2009]

$\tau$ : tortuosity (-)  
 $F$ : formation factor (-)



## 2 - MULTI-LEVEL CONCEPT APPLIED TO MODELLING OF Cl<sup>-</sup> TRANSPORT IN CONCRETE

\*\*\*\*\*

[Baroghel-Bouny et al., CCC, 2009]

- Multi-level platform (1-D physical numerical model) ●

➔ **4 levels of sophistication**

- Level 1 - Chloride diffusion model (sat. cond.)

- Cl<sup>-</sup> diffusion (in diluted solution) → **Fick's 1<sup>st</sup> law**
- (global) Cl<sup>-</sup> binding → **Freundlich's** non-linear isotherm
- empirical law  $D_{Cl^-} = f(c_{Cl^-})$

(Equil.) thermodynamic modelling

[Johannesson et al., M&S, 2007]

[Hosokawa & Yamada, C&S, 2009]

[Lothenbach et al., CCR, 2010]

- Level 2 - Multi-species transport model (sat. cond.)

- **4 ions + electrical interactions** between ions → **Nernst-Planck/Poisson eq.**
- equil. Cl<sup>-</sup> binding → **various options**

- Level 3 - Advanced physical-chemical model (sat. cond.)

- **6 to 8 ions + 3 to 8 solid compounds**
- Cl<sup>-</sup> binding → **physical adsorption** onto C-S-H + **Friedel's salt formation** by (instant.) chemical reactions (dissol./precip.)
- **microstructural** (and transport property) **changes** (induced by *Friedel's* salt precipitation, Ca(OH)<sub>2</sub> dissolution, ...)

transport-chemistry coupling

- Level 4 - Coupled moisture-ion transport model

- ➔ contribution of **advection** to the overall ionic transport
- ➔ multi-species transport model (**level 2**) extended to **non-sat. cond.**

Increasing level of sophistication



## 2 - MULTI-LEVEL CONCEPT APPLIED TO MODELLING OF Cl<sup>-</sup> TRANSPORT IN CONCRETE

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[Baroghel-Bouny et al., CCC, 2009]

- Multi-level platform (1-D physical numerical model) •

➔ **4 levels of sophistication**

Chemical equilibria ( <i>Friedel's salt formation</i> )	$-\log K$
$\text{H}_2\text{O} \rightleftharpoons \text{H}_3\text{O}^+ + \text{OH}^-$	14
$\text{Ca}(\text{OH})_2 \rightleftharpoons \text{Ca}^{2+} + 2\text{OH}^-$	5,05
$3\text{CaO} \cdot \text{Al}_2\text{O}_3 + 6\text{H}_2\text{O} \rightleftharpoons 3\text{Ca}^{2+} + 4\text{OH}^- + 2\text{Al}(\text{OH})_4^-$	22,5
$3\text{CaO} \cdot \text{CaCl}_2 \cdot \text{Al}_2\text{O}_3 \cdot 10\text{H}_2\text{O} \rightleftharpoons 4\text{Ca}^{2+} + 4\text{OH}^- + 2\text{Al}(\text{OH})_4^- + 2\text{Cl}^-$	29,1

additional eqs associated with dissol./precip. reactions

- Level 2 - Multi-species transport model (sat. cond.)

- 4 ions + electrical interactions between ions → *Nernst-Planck/Poisson eq.*
- equil. Cl<sup>-</sup> binding → various options

- Level 3 - Advanced physical-chemical model (sat. cond.)

- 6 to 8 ions + 3 to 8 solid compounds
- Cl<sup>-</sup> binding → physical adsorption onto C-S-H + *Friedel's salt formation* by (instant.) chemical reactions (dissol./precip.)
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- ➔ contribution of **advection** to the overall ionic transport
- ➔ multi-species transport model (**level 2**) extended to **non-sat. cond.**

Increasing level of sophistication

Transport-chemistry coupling



## 2.2 - ADVANCED PHYSICAL-CHEMICAL MODEL (SAT. COND.)

\*\*\*\*\*

Level 3

- Transport and mass balance equations •

\* Ions:  $\text{Cl}^-$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{OH}^-$ ,  $\text{Ca}^{2+}$ ,  $\text{Al}(\text{OH})_4^-$ , ...

\* Solid compounds:  $\text{Ca}(\text{OH})_2$ , equiv. aluminates, *Friedel's salt*

\* Transport of each ion → *Nernst-Planck equation*

$$\text{Flux (mol.m}^{-2}.\text{s}^{-1}) \rightarrow J_i = -D_i \text{grad} c_i + c_i \text{grad}(\ln \gamma_i) + \frac{z_i F}{RT} c_i \text{grad} \Psi$$

$D_i$  (m<sup>2</sup>.s<sup>-1</sup>): effective ionic diffusion coef. of the saturated mat.  
 $\ln \gamma_i$ : chemical activity coef. (-)  
 $\Psi$ : local elec. potential (V)

\* Mass balance equation for each element (in ion or solid compound)

$$\frac{\partial}{\partial t} [\phi c_i + s_i] + \text{div} J_i = 0$$

[Nguyen et al., RILEM, 2006]  
 [Nguyen et al., ICC'07, 2007]

Transport-chemistry coupling

Microstructural evolution



Transport property changes

Porosity

$$\phi = \phi_0 + \sum v_i \Delta s_i$$

$s_i$ : amount of solid compound  $i$  (mol / m<sup>3</sup> of mat.)  
 $v_i$ : molar vol. of solid compound  $i$  (m<sup>3</sup> / mol)

Effective diffusion coef.

$$D_i = D_i^0 \frac{\phi}{\phi_0} \left( \frac{\phi_0 - 0.18}{\phi - 0.18} \right)^2$$

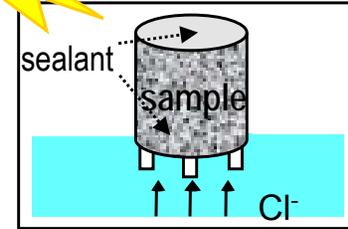
derived from [Bentz et al., CCA, 1998]

# 2.2 - ADVANCED PHYSICAL-CHEMICAL MODEL (SAT. COND.)

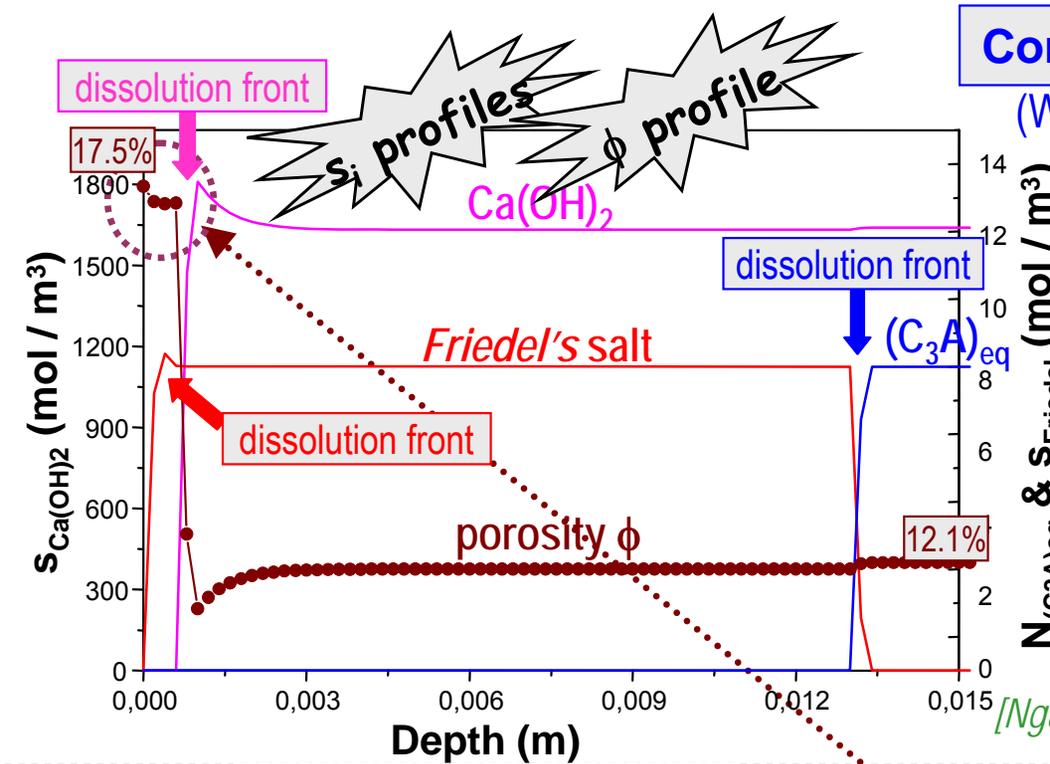
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Level 3

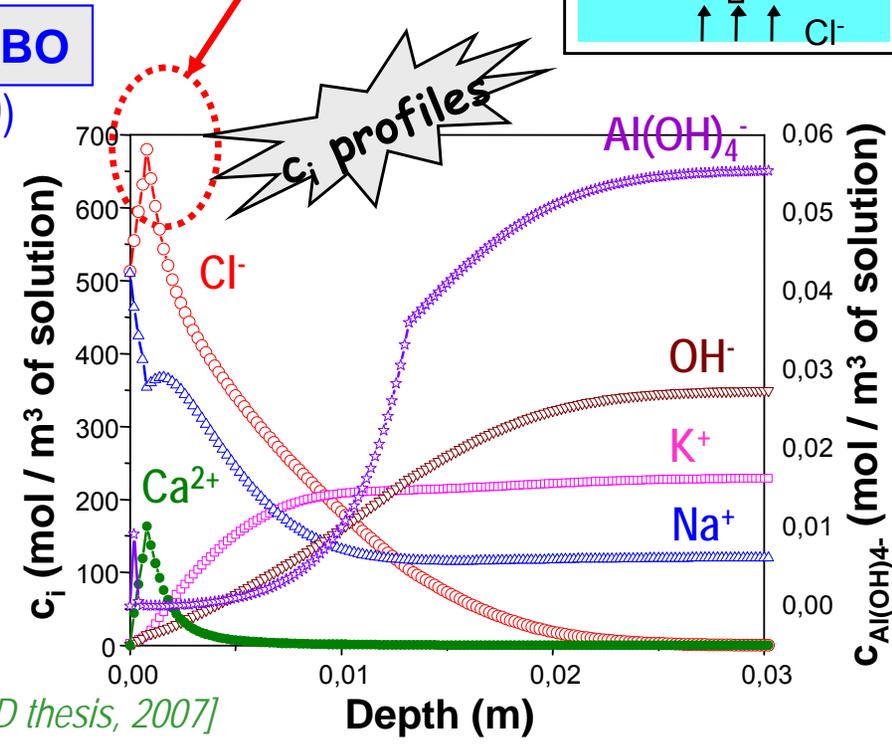
- Example of simulations (nss diffusion test in lab)



- **B.C.:** 90-day exposure to 30 g.L<sup>-1</sup> NaCl (i.e.  $c_{Cl^-} = 517$ ,  $c_{Na^+} = 517$  mol.m<sup>-3</sup>)

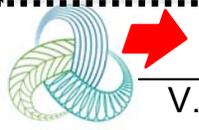


**Concrete BO**  
(W/C=0.49)



[Nguyen, Ph.D thesis, 2007]

- Cl<sup>-</sup> ingress → aluminates dissolution → Friedel's salt precipitation
- **B.C.:** → Ca(OH)<sub>2</sub> dissolution → porosity ↑ in the surf. zone
- c<sub>Ca2+</sub> ↑ → c<sub>Cl-</sub> ↑ in the surf. zone (> B.C.) (Friedel's salt dissolution)



Evolution of pore solution & solid phase composition and of microstructure

## 2 - MULTI-LEVEL CONCEPT APPLIED TO MODELLING OF Cl<sup>-</sup> TRANSPORT IN CONCRETE

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[Baroghel-Bouny et al., CCC, 2009]

- Multi-level platform (1-D physical numerical model) ●

➔ **4 levels of sophistication**

- Level 1 - Chloride diffusion model (sat. cond.)

- Cl<sup>-</sup> diffusion (in diluted solution) → **Fick's 1<sup>st</sup> law**
- (global) Cl<sup>-</sup> binding → **Freundlich's** non-linear isotherm
- empirical law  $D_{Cl^-} = f(c_{Cl^-})$

[Nilsson et al., 1996]

[Johannesson, CCR, 2003]

[Samson, 2005]

- Level 2 - Multi-species transport model (sat. cond.)

- **4 ions + electrical interactions** between ions → **Nernst-Planck/Poisson eq.**
- equil. Cl<sup>-</sup> binding → **various options**

- Level 3 - Advanced physical-chemical model (sat. cond.)

- **6 to 8 ions + 3 to 8 solid compounds**
- Cl<sup>-</sup> binding → **physical adsorption** onto C-S-H + **Friedel's salt formation** by (instant.) chemical reactions (dissol./precip.)
- **microstructural** (and transport property) **changes** (induced by *Friedel's* salt precipitation, Ca(OH)<sub>2</sub> dissolution, ...)

- Level 4 - Coupled moisture-ion transport model

- ➔ contribution of **advection** to the overall ionic transport
- ➔ multi-species transport model (**level 2**) extended to **non-sat. cond.**

**Non-saturated conditions**

Increasing level of sophistication



# 2.3 - COUPLED MOISTURE-ION TRANSPORT MODEL

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• Description •

**Level 4**

For (concentrated) non-ideal sol.

$$\ln a_w = f(I)$$

*I*: ionic strength of the solution (mol.m<sup>-3</sup>)

$$p_c = -\frac{\rho_w}{M_w} RT \left[ \ln \frac{p_v}{p_{vs}(T)} - \ln a_w \right]$$

h: relative humidity (-)

[Lin & Lee, FPE, 2003]

degree of saturation

[Baroghel-Bouny et al., CCR, 1999]  
[Thiery et al., REGC, 2007]

Moisture transport

- ionic transport → **Nernst-Planck/Poisson eq.** (incl.  $\gamma$  effects)
- liquid phase & gas movement → **extended Darcy's law**
- water vapour & dry air relative diffusion → **Fick's 1<sup>st</sup> law**
- water-ions coupling → water activity  $a_w$  → **extended Kelvin's law**
- transport properties variations vs.  $S_l$
- { equil. Cl<sup>-</sup> binding → various options  
+ possible **delay effect**

*integral or analytical laws*  
e.g. permeabilities → [Mualem, 1976]

*kinetics equation*

$$d\bar{s}_{Cl}^*/dt = - (\bar{s}_{Cl}^* - \mu_{Cl} \gamma) / \tau$$

*characteristic (delay) time*  
[Francy, Ph.D thesis, 1998]

→ multi-species & multi-phase!

→ natural drying, wick action, **wetting-drying cycles**, ... → tidal zones



# 2.3 - COUPLED MOISTURE-ION TRANSPORT MODEL

\*\*\*\*\*

[Baroghel-Bouny et al., CCR, 2011]

Level 4

- Transport and mass balance equations

\* Ions: Cl<sup>-</sup>, OH<sup>-</sup>, Na<sup>+</sup>, K<sup>+</sup>

account for chemical activity effects

\* Transport of each ion → Nernst-Planck equation

$$Flux \ (mol.m^{-2}.s^{-1}) \rightarrow J_i = -D_i \cdot d_{ri}(S_l) \left[ grad c_i + c_i \cdot grad(\ln \gamma_i) + \frac{z_i F}{RT} c_i \cdot grad \Psi \right]$$

effective ionic diffusion coef. of the saturated mat. (constant)

relative diffusion coef.

$$d_{rCl^-} = D_{Cl^-}(S_l) / D_{Cl^-}(S_l = 1) = S_l^\lambda$$

and

$$\text{at } S_l = 1 \quad (i \neq Cl^-) \quad \frac{D_i}{D_i^0} = \frac{D_{Cl^-}}{D_{Cl^-}^0} (= \tau \cdot \phi) = \frac{1}{F}$$

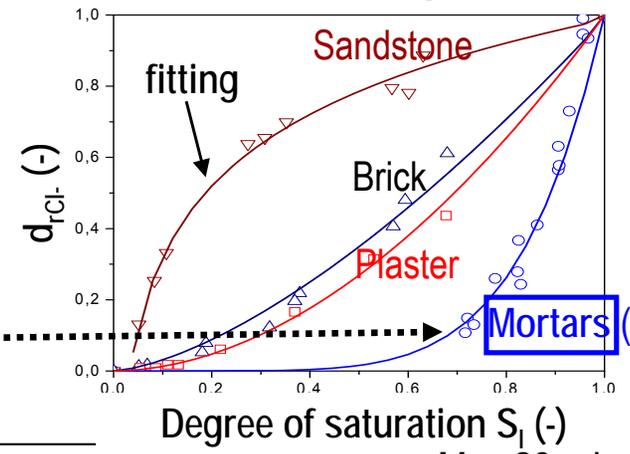
[Samson, 1999]

at infinite dilution

τ : tortuosity (-)  
F : formation factor (-)

[Francy, Ph.D thesis, 1998]

Calibration → λ = 6



# 2.3 - COUPLED MOISTURE-ION TRANSPORT MODEL

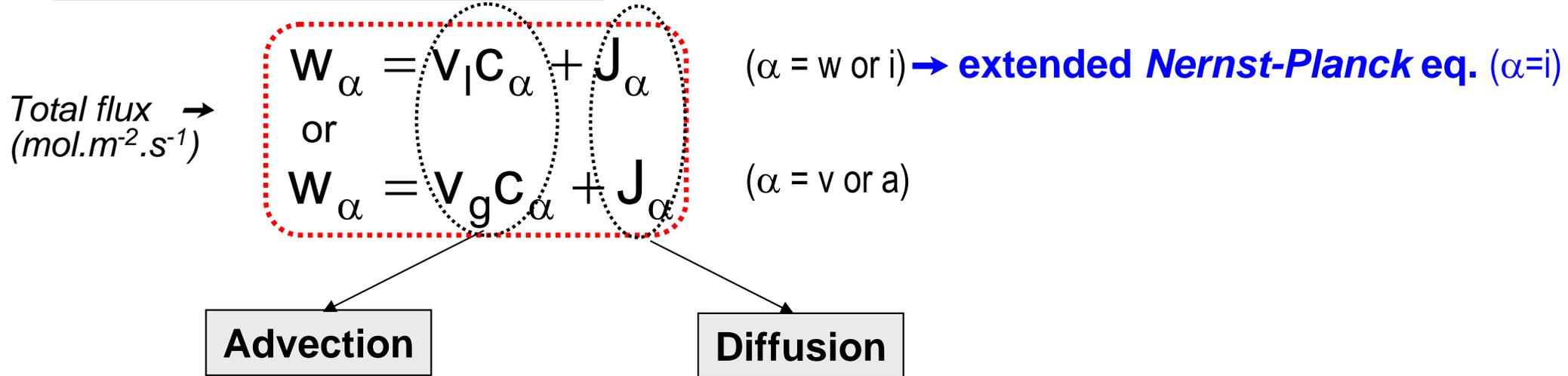
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[Baroghel-Bouny et al., CCR, 2011]

Level 4

- Transport and mass balance equations

## \* Overall transport equation



$c_\alpha$ : conc. in phase  $\alpha$  (mol.m<sup>-3</sup>) with  $\sum v_\alpha c_\alpha = 1$  when  $\alpha = w$  or  $i$ , where  $v_\alpha$  is the molar vol. of phase  $\alpha$  in sol. (m<sup>3</sup>.mol<sup>-1</sup>)

## \* Mass balance equations (for moisture w+v, dry air a, and species j in ion or in solid compound)

$$\frac{\partial}{\partial t} \left( \phi S_l c_w + \phi(1-S_l) \frac{\rho_v}{M_v} \right) = -\text{div}(w_w + w_v)$$

$$\frac{\partial}{\partial t} \left( \phi(1-S_l) \frac{\rho_a}{M_a} \right) = -\text{div}(w_a)$$

$$\frac{\partial}{\partial t} \left( \underbrace{\phi S_l c_j}_{\text{bound}} + \underbrace{s_j}_{\text{free}} \right) = -\text{div}(w_j)$$

porosity (constant)

$s_{Cl}$ : total amount of bound Cl<sup>-</sup> (mol / m<sup>3</sup> of mat.) and  $s_j=0$  for  $j \neq Cl$

$S_{Cl} = S_{Cl}(c_{Cl-})$

$\rightarrow$  **Cl<sup>-</sup> binding isotherm**

e.g. **Freundlich's formula**:  $S_{Cl} = \mu c_{Cl-}^\gamma$

at equilibrium

$n_j$ : total content (mol / m<sup>3</sup> of mat.)

# 2.3 - COUPLED MOISTURE-ION TRANSPORT MODEL

\*\*\*\*\*

- Input data required for the model

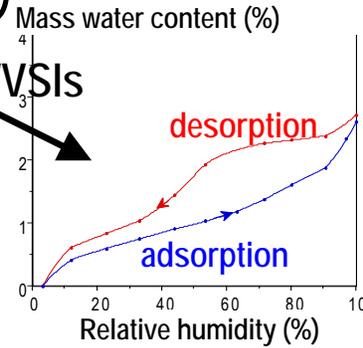
Level 4

Durability indicators

few inputs

$\phi$	Porosity accessible to water ( $m^3.m^{-3}$ )
$D_{Cl^-}$	Effective $Cl^-$ dif. coef. in saturated cond. ( $m^2.s^{-1}$ )
$K_g, K_l$	"Intrinsic" permeabilities ( $m^2$ )
$s_{Cl} = s_{Cl}(c_{Cl^-})$	$Cl^-$ binding isotherm (in sat. cond.) at equilibrium
$p_c = p_c(S_l)$	Capillary pressure curve → derived from exp. WVSIs
$S_l^0$	Initial degree of saturation (-)
$c_{Na^+}^0, c_{K^+}^0, c_{OH^-}^0$	Initial chemical compo. of the pore solution ( $c_{Cl^-}^0=0$ )

exp. or anal. formula or num. inverse analysis



I.C.

+ B.C.: ionic conc. of the contact solution,  $S_l$  at the boundary of the test specimen,  $T^\circ$  (constant), ...

$c_{Na^+}^0, c_{K^+}^0$ : mix-compo. + cement chem. compo. + initial alkali binding [Taylor, ACR, 1987]  
 + hydration model + sat. sol. compo. +  $S_l^0$   
 $c_{OH^-}^0 = c_{Na^+}^0 + c_{K^+}^0$  [Mounanga et al., CCR, 2004]  
 [Nguyen, PhD thesis, 2009]



## 2.3 - APPLICATION OF THE MODEL: UNDERSTANDING & PREDICTION OF **COMPLEX PROCESSES**

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- Simulation of wetting by a NaCl solution (after drying) •

Level 4

Mortar M1N

(W/C=0.50)

### Experimental conditions

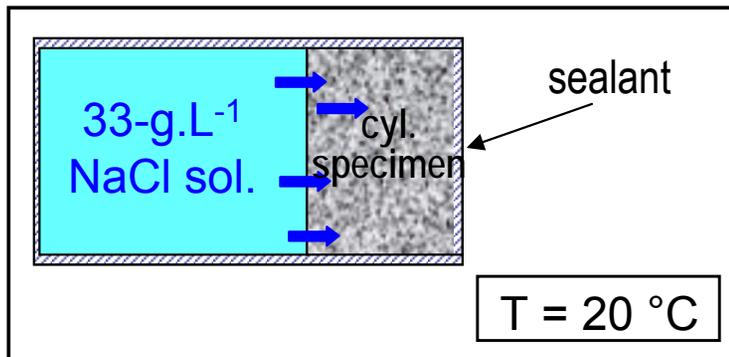
### Material properties

1) 90-day water curing

2) drying at RH=4%

↳ I.C.:  $S_1^0 = 0.09$   
 $c_{Cl^-}^0 = 0, c_{OH^-}^0 = 722, c_{Na^+}^0 = 144,$   
 $c_{K^+}^0 = 578 \text{ mol.m}^{-3}$

3) 24-h expo. to **33 g.L<sup>-1</sup> NaCl + 1 g.L<sup>-1</sup> NaOH**  
 + **4.65 g.L<sup>-1</sup> KOH** by 1 face



[Francy, Ph.D thesis, 1998]

- $\phi = 0.13 \rightarrow \text{exp.}$
- $D_{Cl^-} = 2.1 \cdot 10^{-12} \text{ m}^2.\text{s}^{-1}$  ( $[Cl^-]_{\text{tot}}$  profile after 7-d nss diffusion test  $\rightarrow$  **inv. analysis**)
- $K_1 = 15 \cdot 10^{-21} \text{ m}^2$  (drying kinetics at RH = 4%  $\rightarrow$  **inv. analysis**)
- $p_c = p_c(S_1)$  from **exp. WVAI** [Bonnet, Ph.D thesis, 1997]
- $S_{Cl} = S_{Cl}(c_{Cl^-}) \rightarrow$  **exp. data + Freundlich's description + delay effect** ( $\tau \approx 6\text{h}$ )

Level 2  
Moisture transport

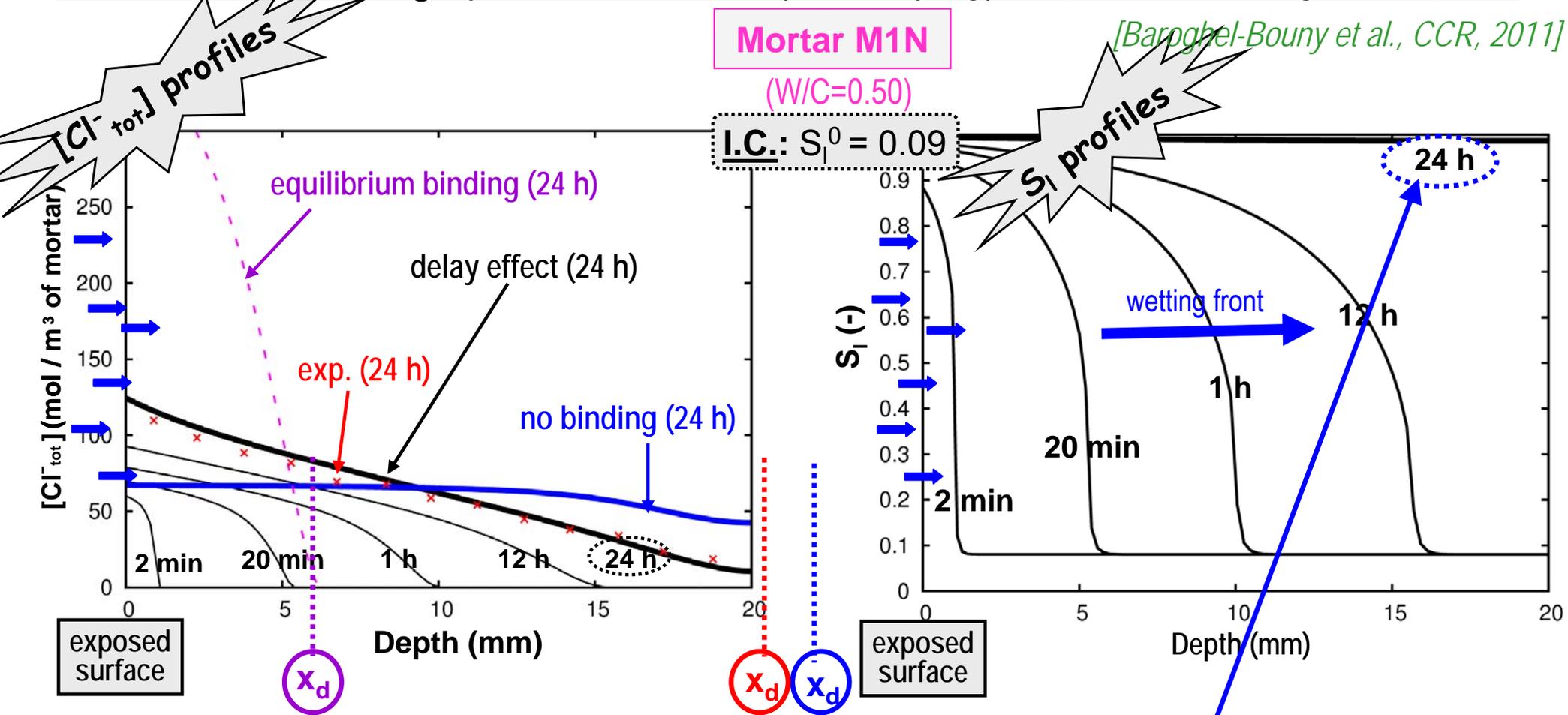
[Francy, Ph.D thesis, 1998]

*high-rate advective transport  
in the short term*



\*\*\*\*\*

• Simulation of wetting by a NaCl solution (after drying): impact of binding description •



• after 24-h exposure → wetting front has reached the specimen boundary  
→  $S_1 = 1$  throughout the specimen thickness

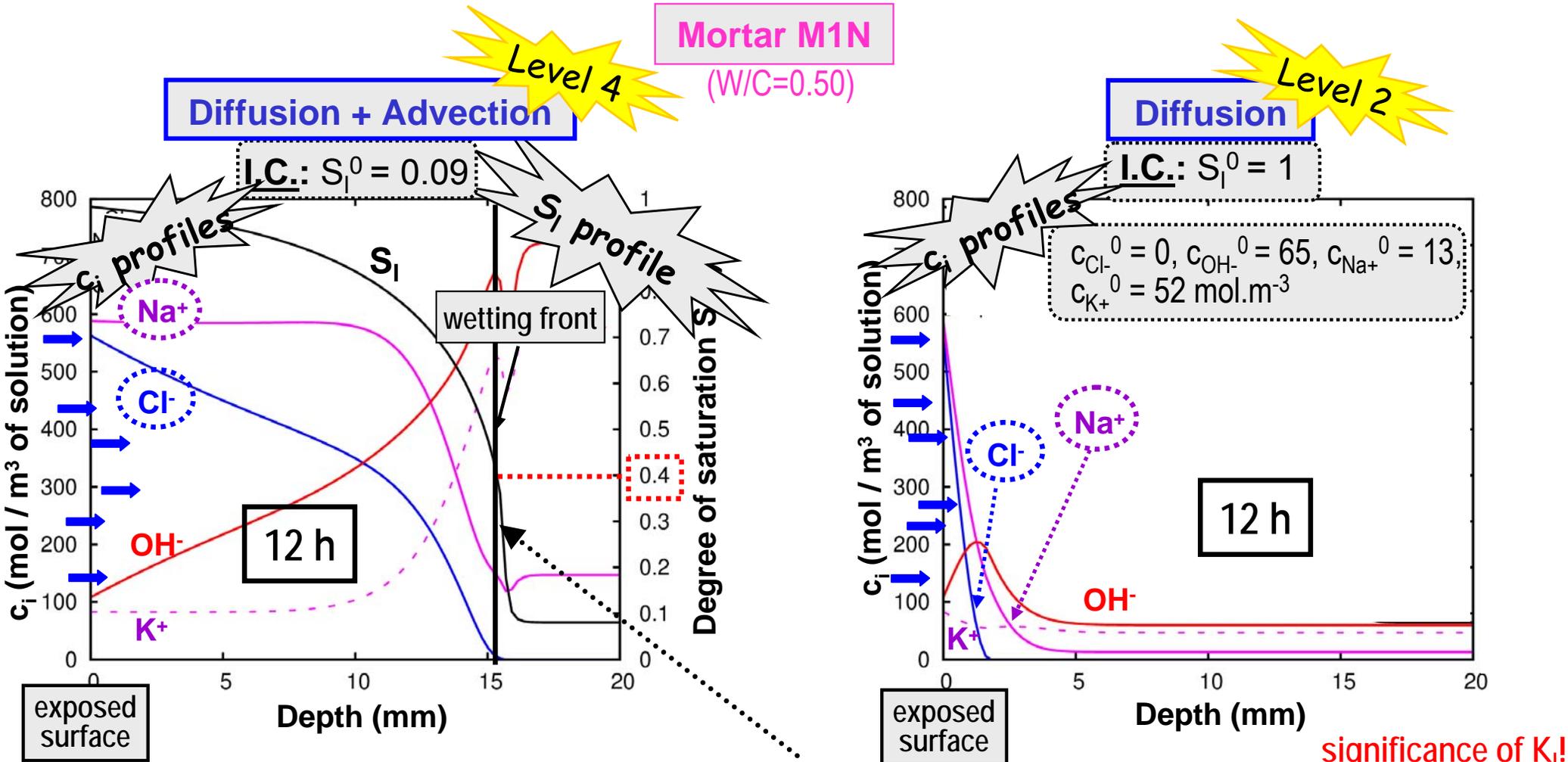
• Freundlich's description + delay effect → best agreement with exp.data

**Models** → importance to account for appropriate Cl<sup>-</sup> binding description (structural safety)

\*\*\*\*\*

[Baroghel-Bouny et al., CCR, 2011]

• Diffusion vs. advection •



→  **$S_l^0 = 0.09$**  | → ions move along with the liquid phase (advection)  
 → faster  $Cl^-$  (and  $Na^+$ ) ingress and higher  $c_{Cl^-}$  compared to  **$S_l^0 = 1$**

→  **$S_l^0 = 1$  (diffusion)** → larger  $Na^+$  penet. depth (no binding) than  $Cl^-$  (equil. binding)

significance of  $K_l$ !



## 2.3 - APPLICATION OF THE MODEL: UNDERSTANDING & PREDICTION OF **COMPLEX PROCESSES**

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### • Simulation of wick-action test •

Level 4

Mortar M1N

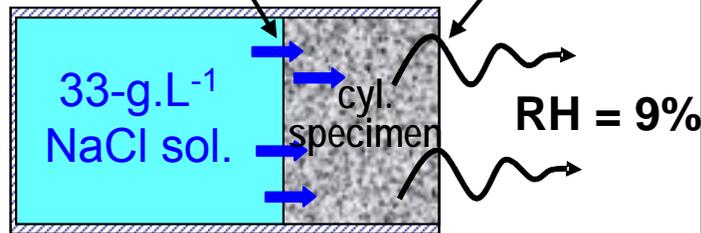
(W/C=0.50)

**Experimental conditions**

upstream surface  
( $x = 0$ )

downstream surface  
( $x = 0.025$  m)

I.C.:  $S_l = 1$



age = 90 days

$T = 20$  °C

[Francy, Ph.D thesis, 1998]

I.C.:  $c_{Cl^-}^0 = 0$ ,  $c_{OH^-}^0 = 65$ ,  $c_{Na^+}^0 = 13$ ,  
 $c_{K^+}^0 = 52$  mol.m<sup>-3</sup>

**Material properties**

- $\phi = 0.13 \rightarrow$  **exp.**
- $D_{Cl^-} = 2.1 \cdot 10^{-12}$  m<sup>2</sup>.s<sup>-1</sup> ( $[Cl^-_{tot}]$  profile after 7-d nss diffusion test  $\rightarrow$  **inv. analysis**)
- $K_l = 15 \cdot 10^{-21}$  m<sup>2</sup> (drying kinetics at RH = 4%  $\rightarrow$  **inv. analysis**)
- $p_c = p_c(S_l)$  from **exp. WVAI & WVDI** [Bonnet, Ph.D thesis, 1997]
- $S_{Cl} = S_{Cl}(c_{Cl^-}) \rightarrow$  **exp. data + Freundlich's description**

Moisture transport

Level 2

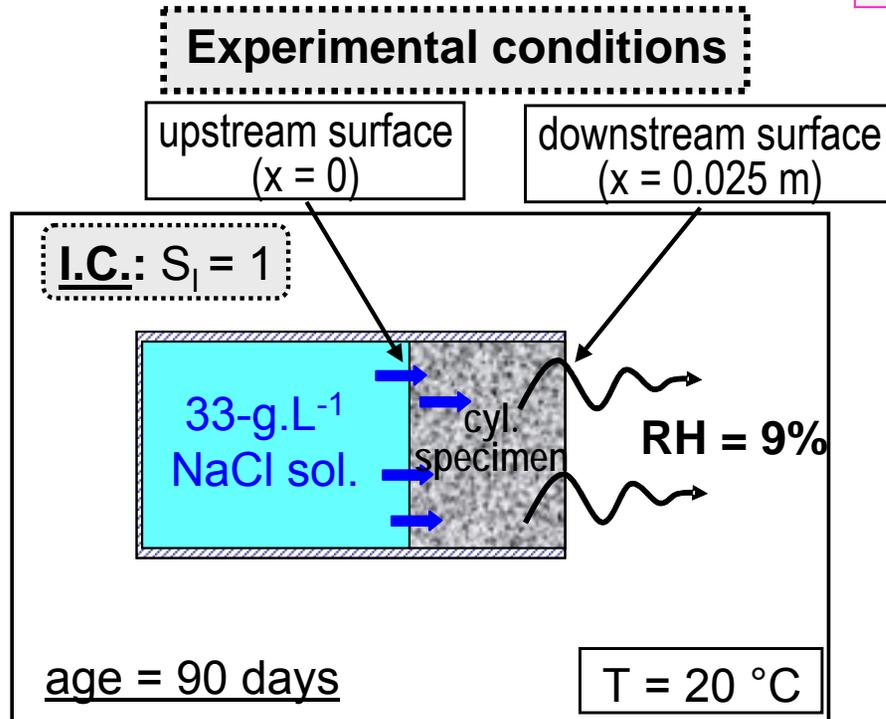
[Francy, Ph.D thesis, 1998]



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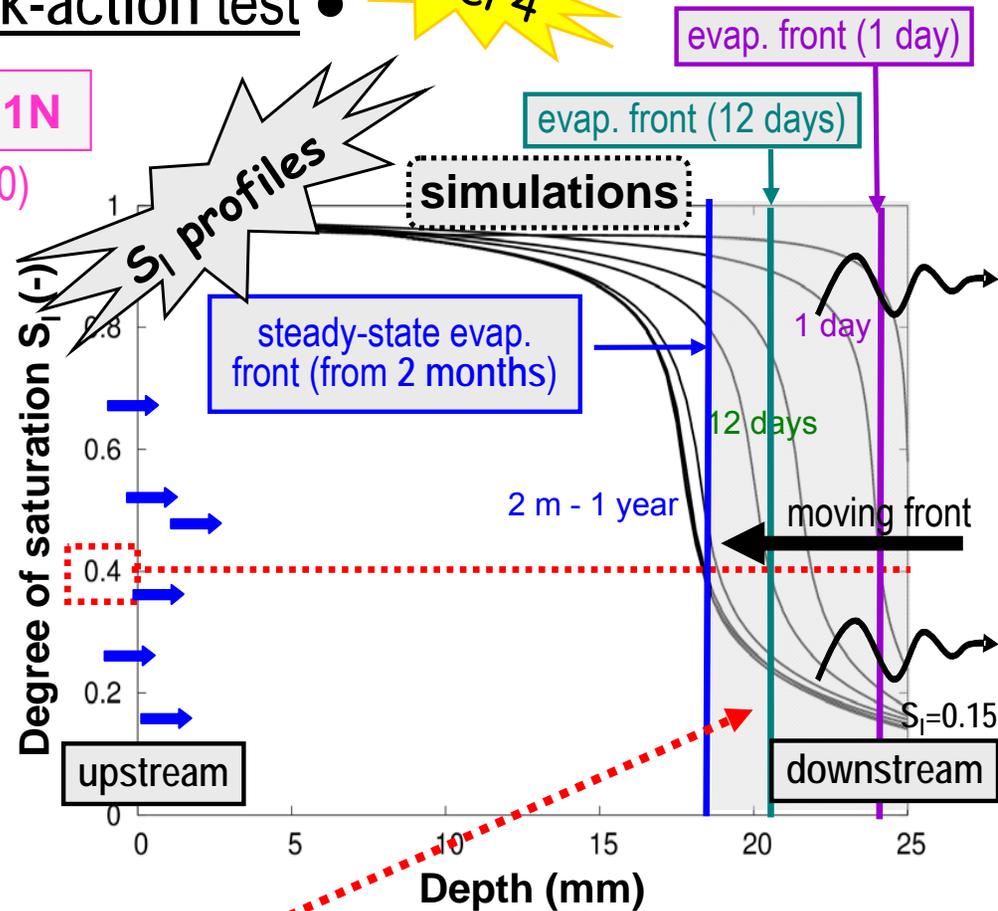
• Simulation of wick-action test •

Level 4



[Francy, Ph.D thesis, 1998]

Mortar M1N  
(W/C=0.50)



[Baroghel-Bouny et al., CCR, 2011]

• RH = 9% at x = 0.025

→ strong drying

→ formation of a zone with  $S_l < 0.40$  (from x = 0.025) → **no liquid transport**

→ **evaporation front**

→ after a given time → **steady-state regime** ( $S_l$  profile & evap. front)



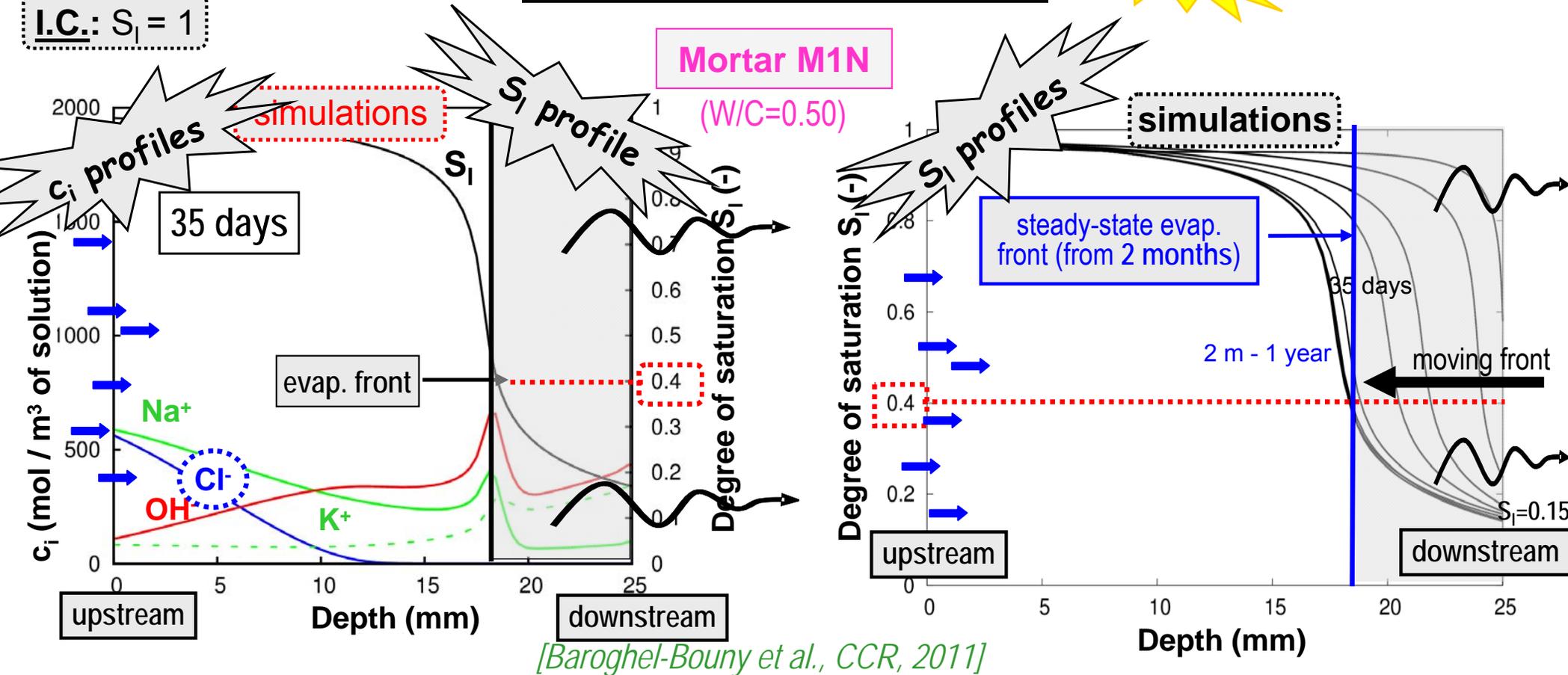
## 2.3 - APPLICATION OF THE MODEL: UNDERSTANDING & PREDICTION OF **COMPLEX PROCESSES**

\*\*\*\*\*

### • Simulation of wick-action test •

Level 4

I.C.:  $S_i = 1$



[Baroghel-Bouny et al., CCR, 2011]

- Close to the upstream surface (x = 0) → Cl<sup>-</sup> move by diffusion + advection towards the downstream surface (x = 0.025)

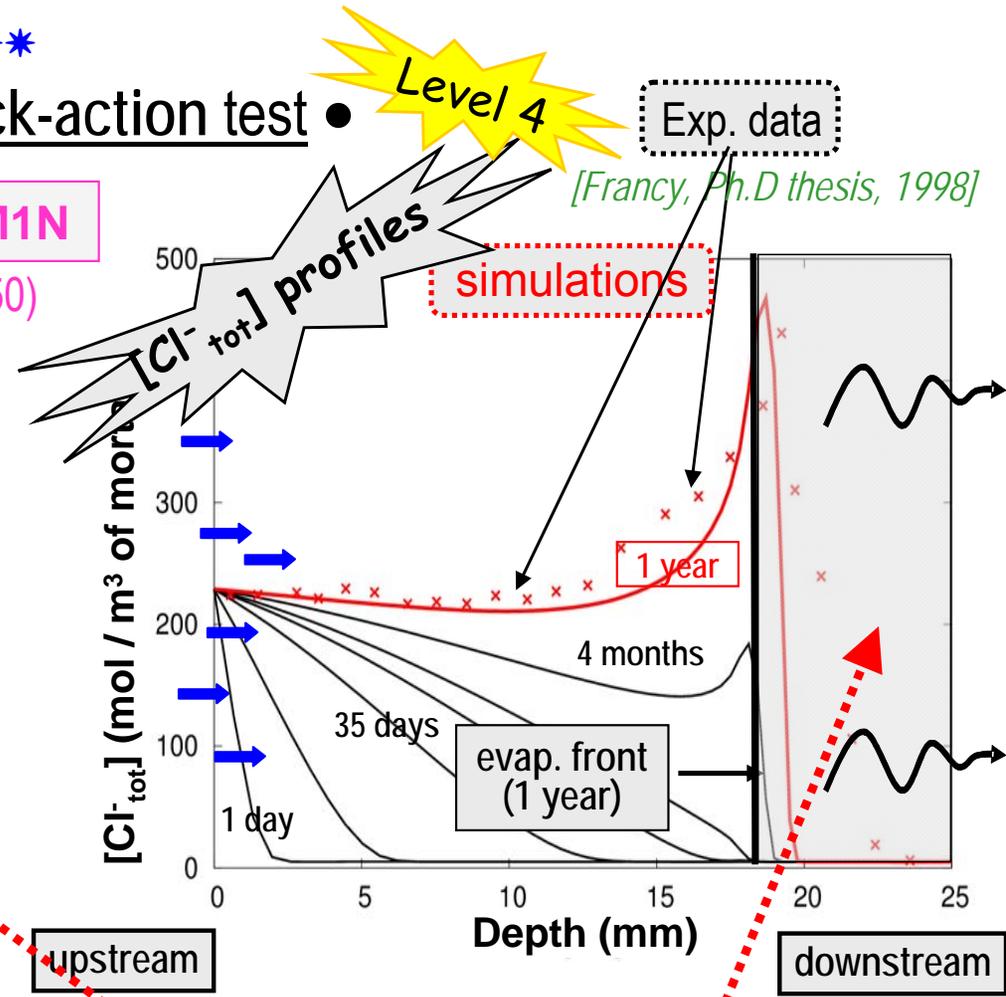
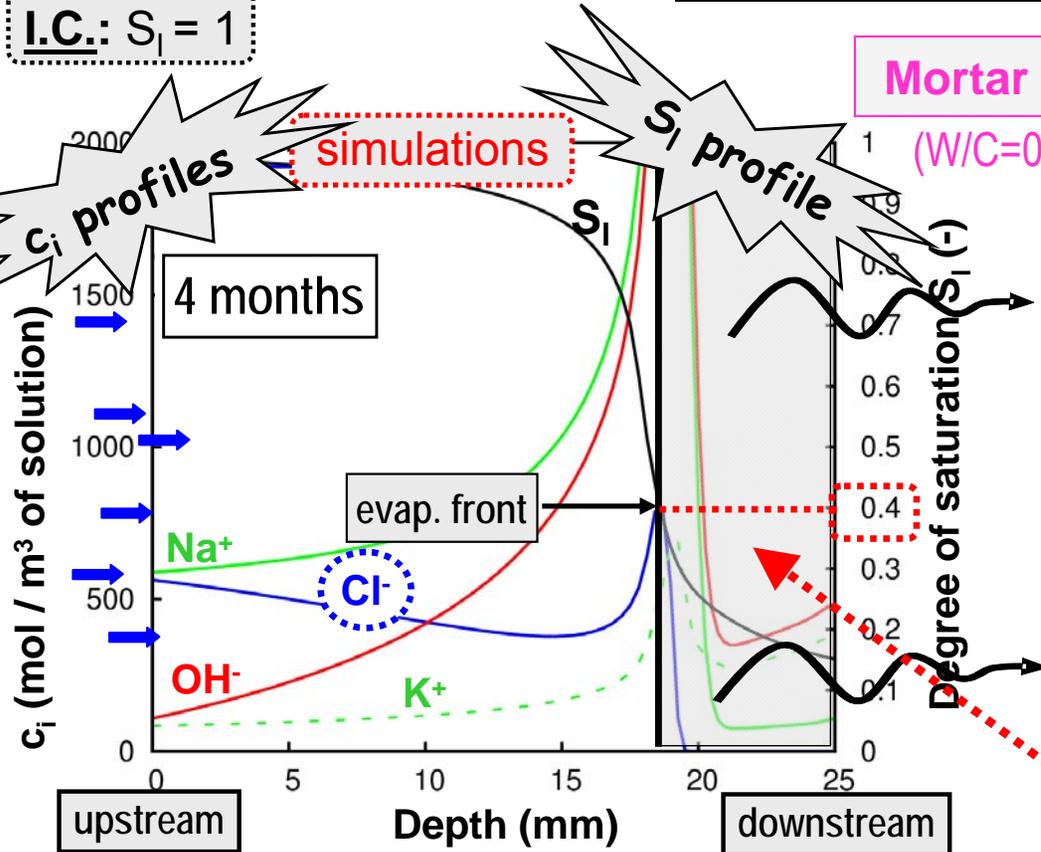


## 2.3 - APPLICATION OF THE MODEL: UNDERSTANDING & PREDICTION OF **COMPLEX PROCESSES**

\*\*\*\*\*

### • Simulation of wick-action test •

I.C.:  $S_l = 1$



[Baroghel-Bouny et al., CCR, 2011]

- Close to the upstream surface ( $x = 0$ ) → **Cl<sup>-</sup>** move by diffusion + advection towards the downstream surface ( $x = 0.025$ )
  - RH = 9% at  $x = 0.025$  → strong drying → significant liquid flow → advection prominent
    - **no liquid transport** in the zone where  $S_l < 0.40$
    - **Cl<sup>-</sup> accumulation** at the evaporation front
- significance of  $K_l$ !**

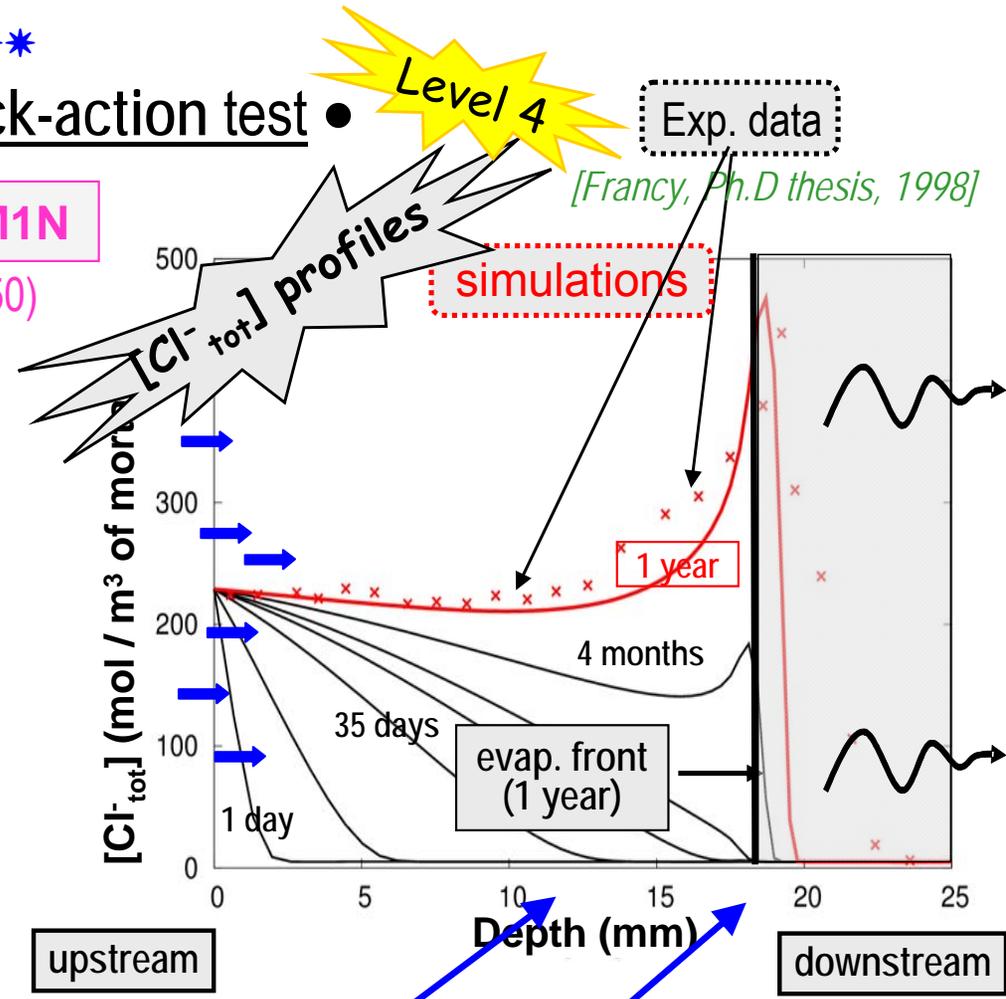
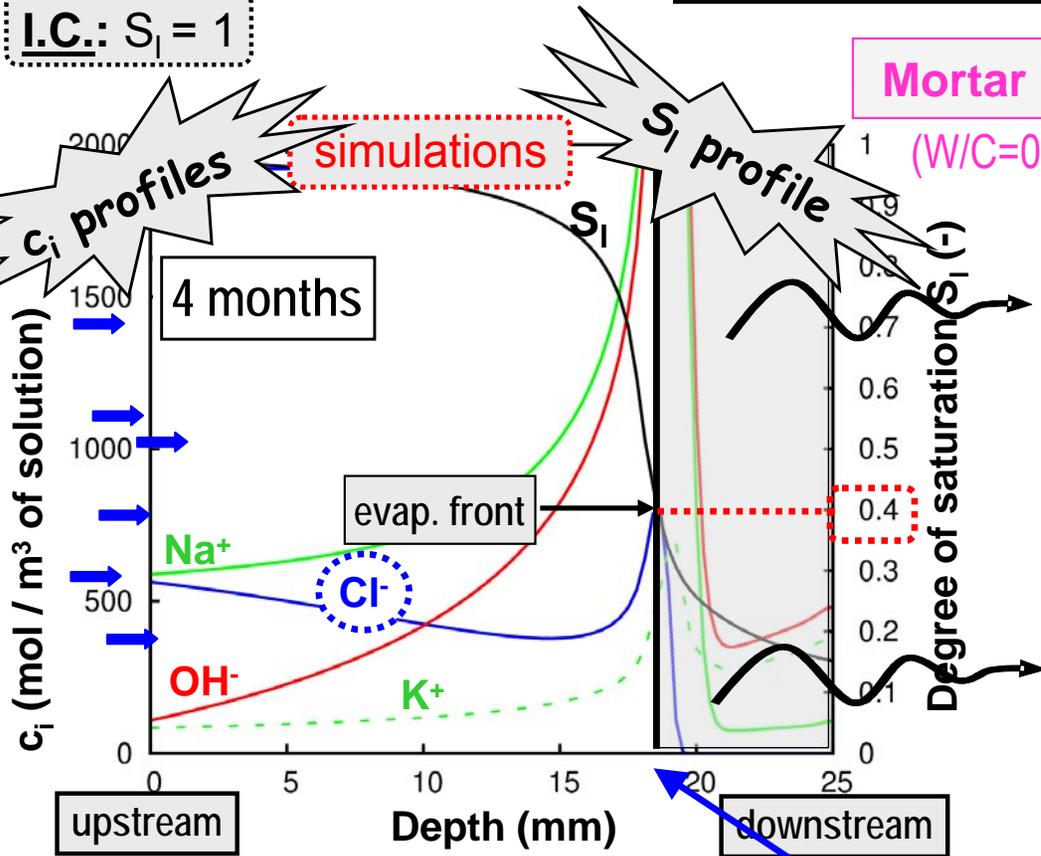


## 2.3 - APPLICATION OF THE MODEL: UNDERSTANDING & PREDICTION OF **COMPLEX PROCESSES**

\*\*\*\*\*

### • Simulation of wick-action test •

**I.C.:**  $S_1 = 1$



[Baroghel-Bouny et al., CCR, 2011]

➡ consistence between **evap. fronts** deduced from  $[Cl^-_{tot}]$ ,  $c_i$  &  $S_1$  profiles

➡ peculiar shape of the num. ionic &  $[Cl^-_{tot}]$  profiles

➡ **good agreement between num. simulations and exp. data (at 1 year)**

↳ location of the **evap. front** **experim.** and **theor.** pointed out

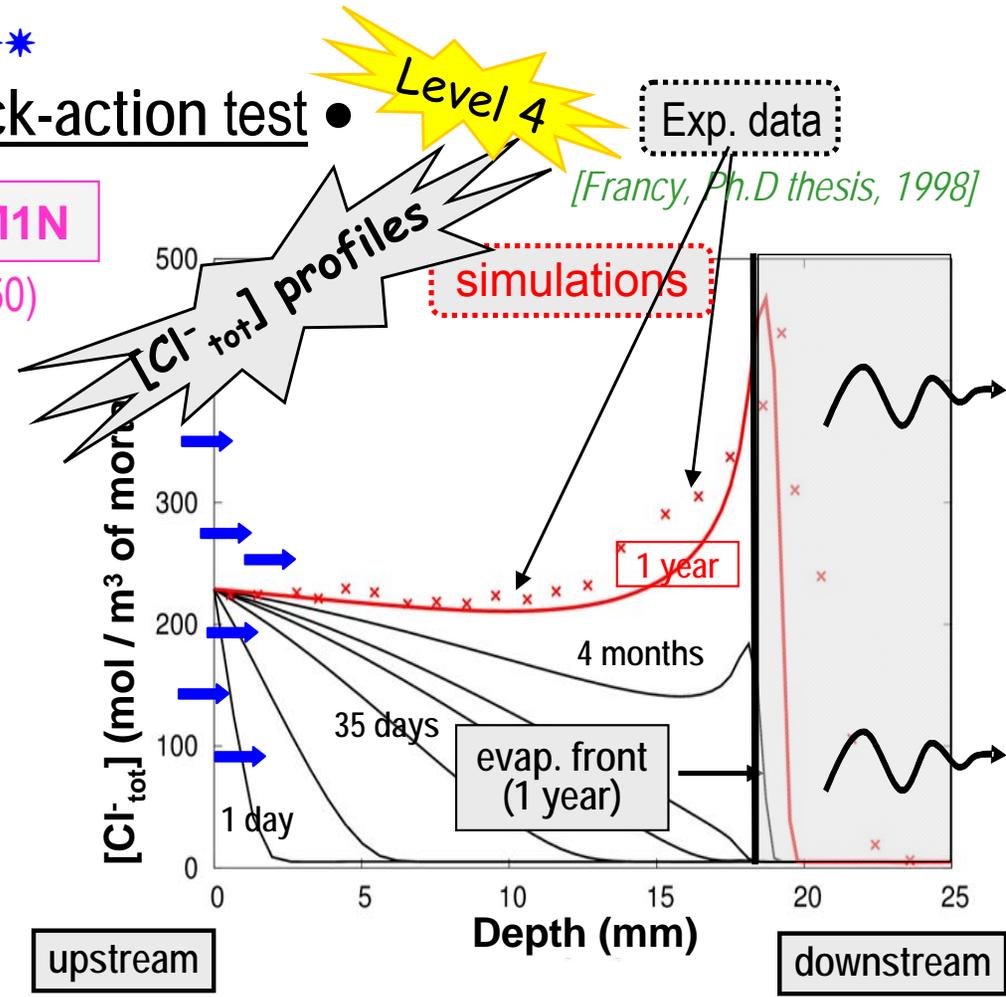
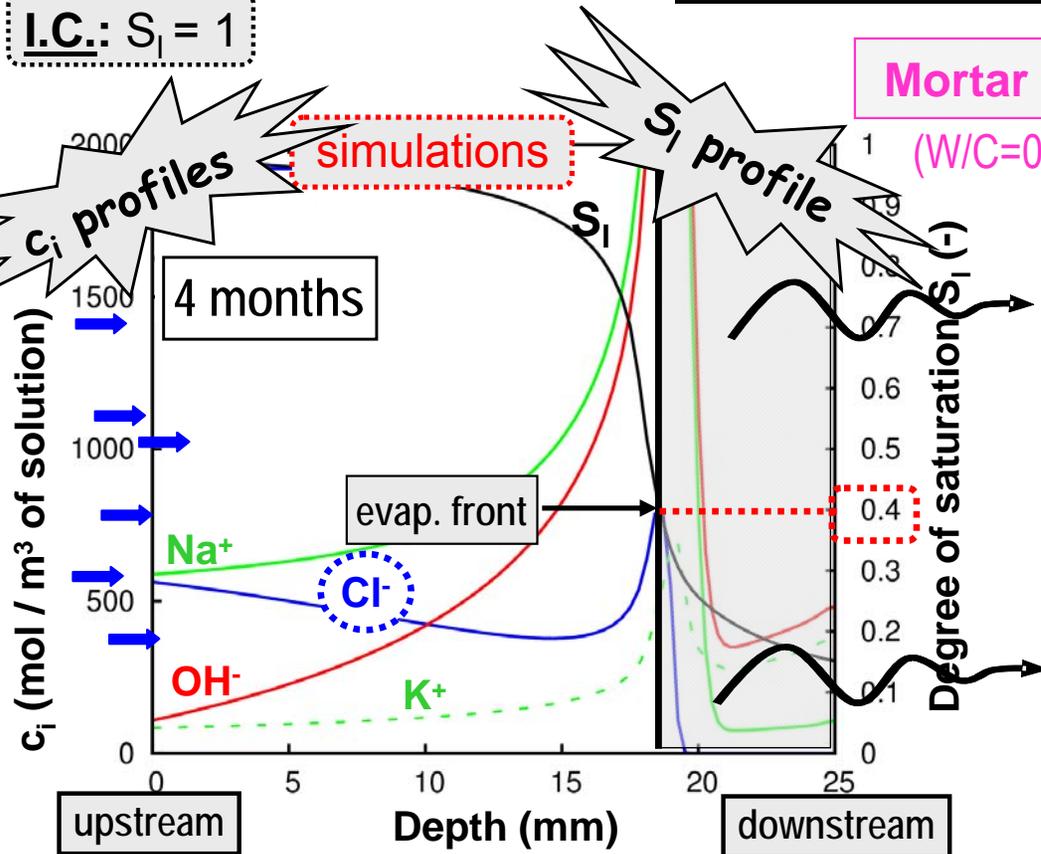


## 2.3 - APPLICATION OF THE MODEL: UNDERSTANDING & PREDICTION OF **COMPLEX PROCESSES**

\*\*\*\*\*

### • Simulation of wick-action test •

I.C.:  $S_l = 1$



[Baroghel-Bouny et al., CCR, 2011]

➔ Simulation of all the complex effects associated with coupled moisture-ion transport on profiles (e.g. in the vicinity of the evap. front)

➔ **Validation of the level-4 model** in lab cond. for prediction  
(1<sup>st</sup> stage of validation)



# Outline

- 1 - Introduction
- 2 - Modelling of isothermal **Cl<sup>-</sup> transport** in concrete
  - 2.1 - Level 2: Multi-species transport model (sat. cond.)
  - 2.2 - Level 3: Advanced physical-chemical model (sat. cond.)
  - 2.3 - Level 4: Coupled moisture-ion transport model
-  3 - ***Modelling of carbonation of concrete***
  - 3.1 - Level 2: Semi-analytical physical-chemical model  
- Probabilistic framework
  - 3.2 - Level 3: Numerical physical-chemical model
- 4 - Concluding remarks & further needed developments



# 3 - MULTI-LEVEL CONCEPT APPLIED TO MODELLING OF CARBONATION OF CONCRETE

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Increasing level of sophistication

• **Level 1 - Analytical physical-chemical models** [Papadakis et al., ACI, 1991]

↳  $\sqrt{t}$  law → sharp carbonation front

**SLD** Easy coupling with probabilistic methods

• **Level 2 - Semi-analytical physical-chemical models**

↳ analytical Papadakis' approach + weathering **cycles** [Bakker, 1993], [Hyvert, 2009]

↳ analytical Papadakis' approach + **numerical** physical moisture transport model + no carbo. for  $RH \geq 90\%$  [Thiery et al., CONMOD'08, 2008]

• **Level 3 - Numerical physical-chemical models**

↳ comprehensive **speciation** models  
thermodynamic (equil.) modelling (+ mod. of hydrodynamic processes in sat. cond.) [van der Lee et al., C&G, 2003], [Matschei, Lothenbach et al., CCR, 2007]

↳ (coupled) **transport-chemistry** models [Steffens, CCR, 2002], [Bary & Sellier, CCR, 2004], [Saetta et al., CCR, 2004], [Mai-Nhu et al., SSCS, 2011]

• thermodynamic modelling → phase assemblages at equilibrium (0-D)  
 - chemistry of the pore solution ( $[K^+]$ ,  $[Na^+]$ , ...) } → pH evolution  
 - evolution of the solid phases (e.g. C-S-H decalcification)

• chemical reaction kinetics ( $Ca(OH)_2$ ) → *soften up the carbonation profile*

• **microstructural** changes → evolution of porosity, transport properties, ...

• coupling with advanced **transport** model (non-sat. cond.) →  $S_i$  evolution

**Advanced models**

**chemistry**

**physics**

[Thiery et al., 2005-2012]

# 3.2 - NUMERICAL PHYSICAL-CHEMICAL MODEL

\*\*\*\*\*

Level 3

[Thiery et al., CANMET/ACI, 2006]

- Chemical aspects: speciation in the pore solution •

local thermodynamical equilibrium

free & bound alkalis are taken into account

	Chemical reactions (aqueous solution)	$\log(K_i)$	$r_i$	← reaction rate
(1)	$OH^- + H^+ \rightleftharpoons H_2O$	14	$r_1$	
(2)	$Ca^{2+} + 2OH^- \rightleftharpoons Ca(OH)_2^0$	0	$r_2$	
(3)	$Ca^{2+} + H_2O \rightleftharpoons Ca(OH)^+ + H^+$	-12.78	$r_3$	
(4)	$Na^+ + H_2O \rightleftharpoons NaOH^0 + H^+$	-14.18	$r_4$	
(5)	$K^+ + H_2O \rightleftharpoons KOH^0 + H^+$	-14.46	$r_5$	
(6)	$CO_2^0 + H_2O \rightleftharpoons H_2CO_3$	-2.77	$r_6$	} $CO_2$ dissol./dissociation in the pore solution
(7)	$H_2CO_3 + OH^- \rightleftharpoons HCO_3^- + H_2O$	7.65	$r_7$	
(8)	$HCO_3^- + OH^- \rightleftharpoons CO_3^{2-} + H_2O$	3.66	$r_8$	
(9)	$Ca^{2+} + HCO_3^- \rightleftharpoons CaHCO_3^-$	1.11	$r_9$	
(10)	$Na^+ + HCO_3^- \rightleftharpoons NaHCO_3^0$	-0.25	$r_{10}$	
(11)	$Na^+ + HCO_3^- \rightleftharpoons NaCO_3^- + H^+$	-9.10	$r_{11}$	
(12)	$H_2SiO_4^{2-} + 2H^+ \rightleftharpoons H_4SiO_4^0$	23.14	$r_{12}$	
(13)	$H_2SiO_4^{2-} + H^+ \rightleftharpoons H_3SiO_4^-$	13.33	$r_{13}$	
(14)	$H_2SiO_4^{2-} + Ca^{2+} \rightleftharpoons CaH_4SiO_4^0$	4.60	$r_{14}$	
(15)	$H_3SiO_4^- + Ca^{2+} \rightleftharpoons CaH_3SiO_4^+$	1.20	$r_{15}$	

↳ evolution of the chemical compo. of the pore solution

↳ pH value



# 3.2 - NUMERICAL PHYSICAL-CHEMICAL MODEL

\*\*\*\*\*

Level 3

[Morandea et al., CONMOD, 2010]

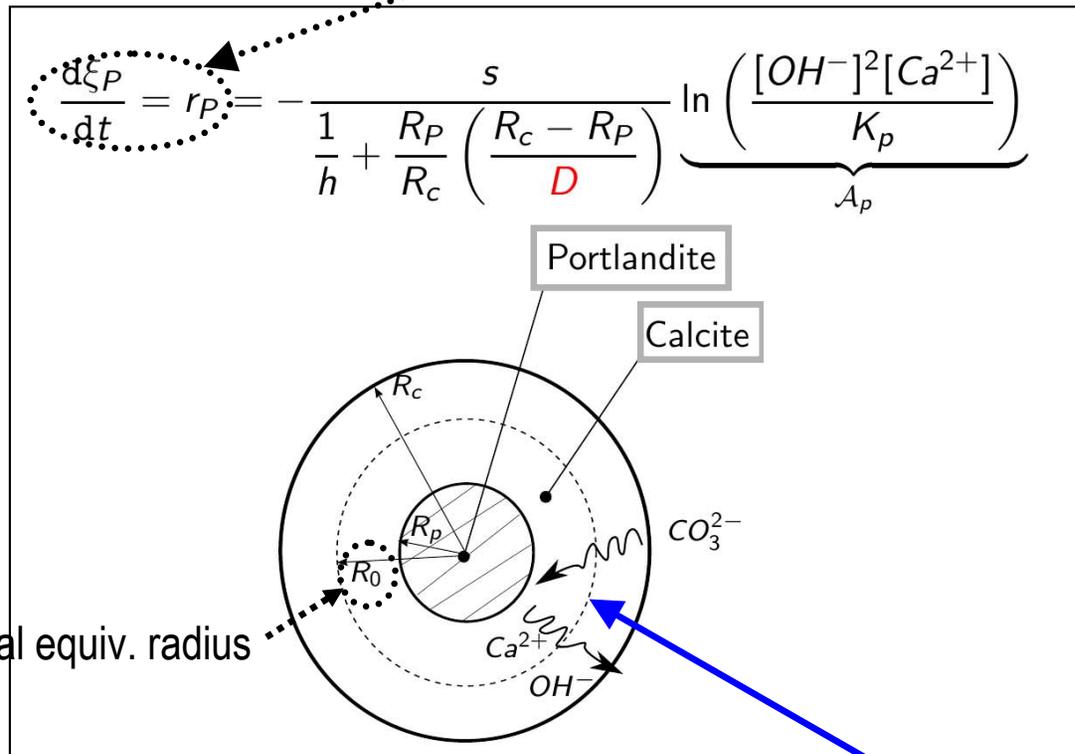
- Chemical aspects: chemical reactions between ionic & solid phases (dissol./precip.) - kinetic effect

evolution of solid phases

	Heterogeneous chemical reactions	$\log(K_i)$	$r_i$
(P)	$Ca^{2+} + 2OH^- \rightleftharpoons CH$	5.19	$r_P$
(C)	$Ca^{2+} + CO_3^{2-} \rightleftharpoons C\bar{C}$	8.45	$r_C$

reaction rate

→  $Ca(OH)_2$  dissolution and  $CaCO_3$  precipitation



→ reduction of accessibility ( $CaCO_3$  layer)

kinetic effect  
softens up the front



# 3.2 - NUMERICAL PHYSICAL-CHEMICAL MODEL

\*\*\*\*\*

Level 3

[Morandea et al., CONMOD, 2010]

- Chemical aspects: chemical reactions between ionic & solid phases (dissol./precip.) - kinetic effect

evolution of solid phases

SCMs!

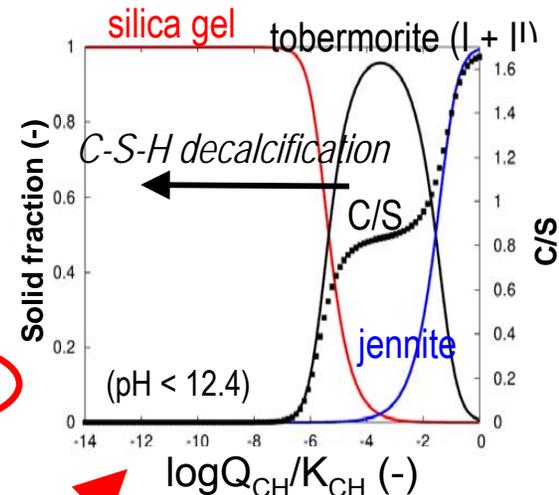
	Heterogeneous chemical reactions	$\log(K_i)$	$r_i$	reaction rate
(P)	$Ca^{2+} + 2OH^- \rightleftharpoons CH$	5.19	$r_P$	
(C)	$Ca^{2+} + CO_3^{2-} \rightleftharpoons C\bar{C}$	8.45	$r_C$	
(C-S-H)	$C_xS_yH_z \rightleftharpoons xCa^{2+} + 2xOH^- + yH_4SiO_4^0 + (z - x - 2y)H_2O$	variable	$r_{CSH}$	

→ progressive decalcification of C-S-H (& CaCO<sub>3</sub> precipitation)

## (Ideal) solid solution model [Kulik & Kersten, JACS, 2001]

2 ideal C-S-H binary solid solution phases  
 ↳ 4 end-members

Amorphous silica:	$C_0S_1H_1$	$C/S = 0$	$\log(K_i) = -2.71$
Tobermorite II:	$C_{1.5}S_{1.8}H_3$	$C/S = 0.83$	$\log(K_i) = -21.19$
Tobermorite I:	$C_2S_{2.4}H_4$	$C/S = 0.83$	$\log(K_i) = -28.26$
Jennite:	$C_{1.5}S_{0.9}H_{2.4}$	$C/S = 1.7$	$\log(K_i) = -15.62$



For each end-member i: molar solid fraction  $f_i = Q_i/K_i$  with  $\sum f_i = 1$   
 activity product      solubility product

↳ constitutive chemical law which depends on  $Q_{CH}$  → easy implementation  
 ↳ pH value



# 3.2 - NUMERICAL PHYSICAL-CHEMICAL MODEL

Level 3

\*\*\*\*\*

- Transport equations (macroscale - partially saturated material) •

[Thiery et al., CANMET/ACI, 2006]

## 1 Gaseous CO<sub>2</sub> diffusion

CO<sub>2</sub> molar flux  $w_{CO_2} = -D_{CO_2}(\phi, S_l) \text{grad} [CO_2]$  (Fick's 1<sup>st</sup> law)

$$D_{CO_2}(\phi, S_l) = D_{CO_2}^0 \phi^{2,74} (1 - S_l)^{4,20}$$

diffusion coef. in the air

reduction factor

## 2 Liquid water transport

filtration rate:  $V_l = -\frac{K_l}{\eta} k_{rl}(S_l) \text{grad} p_l$  (extended Darcy's law)

$p_l(S_l) = p_g - p_c(S_l)$  : capillary pressure curve

## 3 Transport of ionic species (e.g. Ca<sup>2+</sup> from Ca(OH)<sub>2</sub> dissolution)

mole flux of species  $i$ :  $w_i = -D_i \text{grad} [i] - \frac{z_i F}{RT} D_i \text{grad} \psi + [i] V_l$  (extended Nernst-Planck equation)

advection

$$D_i = \frac{D_i^0}{D_{Ca^{2+}}^0} \times 2,35 \cdot 10^{-13} \exp(9,95\phi) \frac{1}{[1 + 625(1 - S_l)^4]}$$

[Tognazzi, 1998], [Thiery, 2005]



## 3.2 - NUMERICAL PHYSICAL-CHEMICAL MODEL

Level 3

\*\*\*\*\*

- Balance equations and related main unknown variables •

[Thiery et al., CANMET/ACI, 2006]

	Equations		Related variables
(1) Global mass balance equation	$\frac{\partial m}{\partial t} = -\text{div } \mathbf{w}_m$	$\iff$	$S$
(2) Charge balance	$\text{div } \mathbf{w}_q = 0$	$\iff$	$\Psi$
(3) C-balance	$\frac{\partial n_C}{\partial t} = -\text{div } \mathbf{w}_C$	$\iff$	$[CO_2]$
(4) Na-balance	$\frac{\partial n_{Na}}{\partial t} = -\text{div } \mathbf{w}_{Na}$	$\iff$	$[Na^+]$
(5) K-balance	$\frac{\partial n_K}{\partial t} = -\text{div } \mathbf{w}_K$	$\iff$	$[K^+]$
(6) Ca-balance	$\frac{\partial n_{Ca}}{\partial t} = -\text{div } \mathbf{w}_{Ca}$	$\iff$	$n_{C\bar{C}}$
(7) Si-balance	$\frac{\partial n_{Si}}{\partial t} = -\text{div } \mathbf{w}_{Si}$	$\iff$	$n_{C-S-H}$
(8) Local electroneutrality	$q = 0$	$\iff$	$[OH^-]$
(9) solid solution model	$\sum_i f_i = 0$	$\iff$	$[H_3SiO_4^-]$

Coupling between transport equations & chemical reactions



# 3.2 - NUMERICAL PHYSICAL-CHEMICAL MODEL

\*\*\*\*\*

Level 3

• Input data required for the model (accelerated carbonation in lab) •

few inputs

Durability indicators

I.C.	$c_{Na^+}^0, c_{K^+}^0$	Initial chemical compo. of the pore solution
	$n_{Ca(OH)_2}^0$	Initial $Ca(OH)_2$ content in concrete ( $mol.m^{-3}$ )
	$n_{C-S-H}^0$	Initial C-S-H content in concrete ( $mol.m^{-3}$ )
	$R_{Ca(OH)_2}^0$	Initial $Ca(OH)_2$ crystal equiv. radius ( $\mu m$ )
	$\phi^0$	Initial porosity accessible to water ( $m^3.m^{-3}$ )
	$K_l^0$	Initial intrinsic permeability to liquid water ( $m^2$ )
	$S_l^0$	Initial degree of saturation (-)
	$p_c = p_c(S_l)$	Capillary pressure curve
B.C.	$x_{CO_2}, RH_{ext.}$	External $CO_2$ concentration ( $mol.m^{-3}$ ) and RH
	$S_l$	Degree of saturation at the boundary of the sample

exp. (TGA)

Chemical

hydration model

literature

Physical

$$K_l = K_l^0 \left[ \frac{\phi}{\phi^0} \right]^3 \left[ \frac{1-\phi}{1-\phi^0} \right]^2$$

[van Genuchten, 1982]



# 3.2 - NUMERICAL PHYSICAL-CHEMICAL MODEL: EXAMPLES OF SIMULATION

Level 3

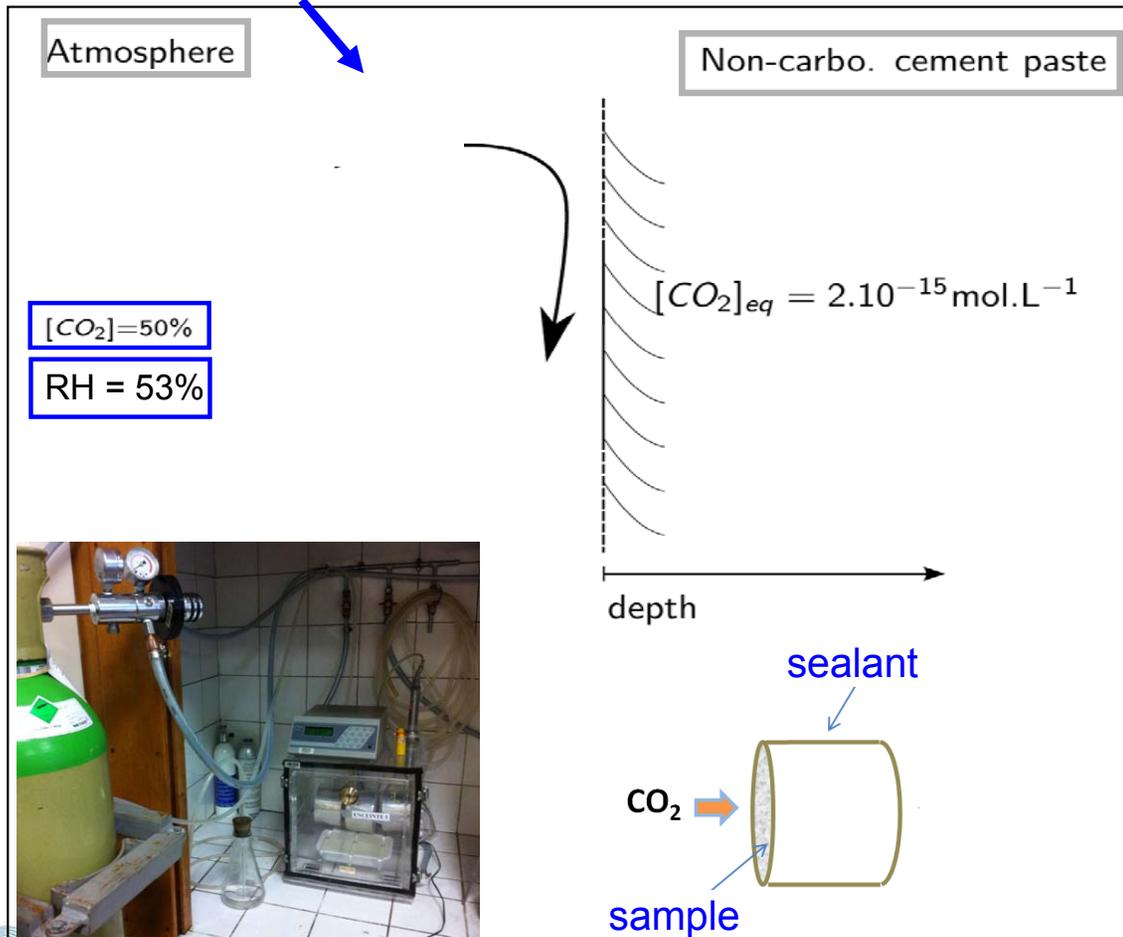
\*\*\*\*\*

Hcp

(CEM I ; W/C=0.45)

(accelerated carbonation in lab)

- 1) 1-year sealed curing
- 2) 1-year exposure to 1-D drying at RH=53%
- 3) **1-D carbonation**



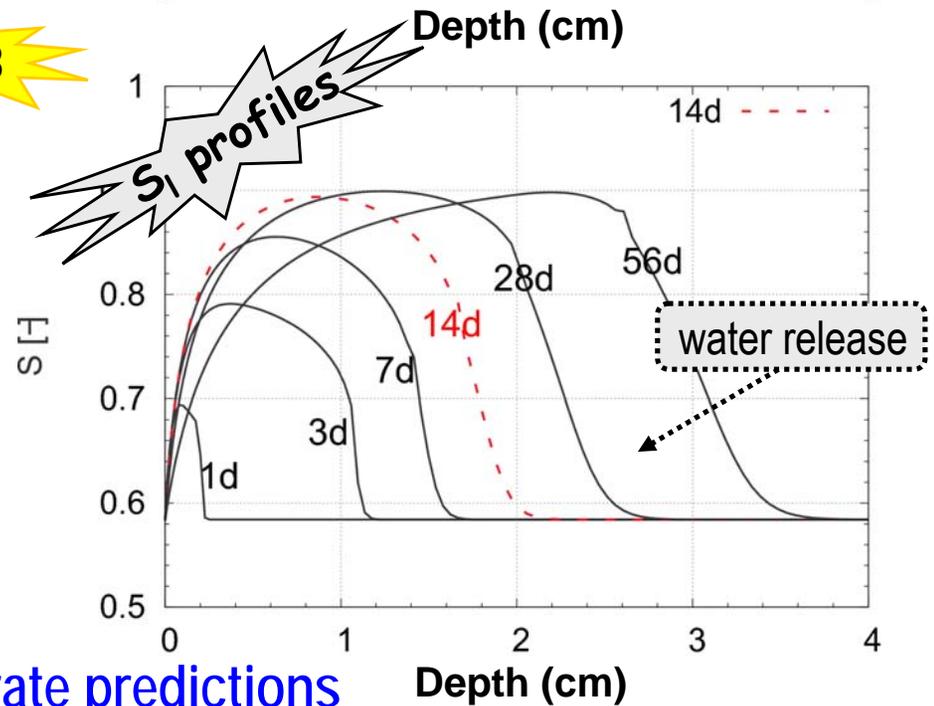
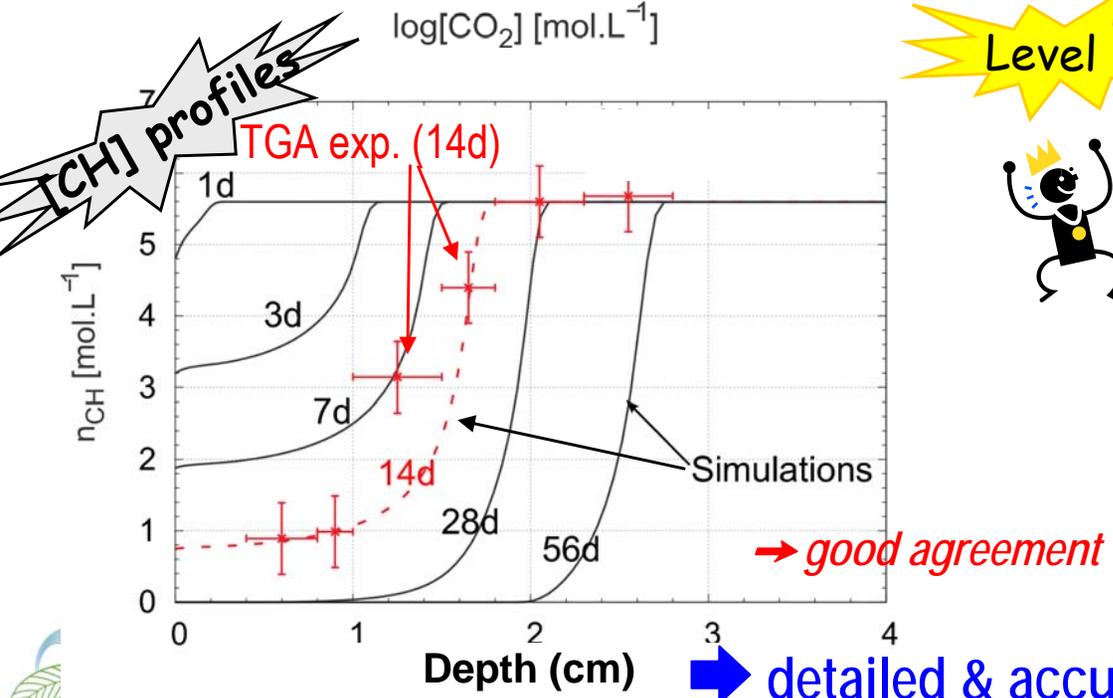
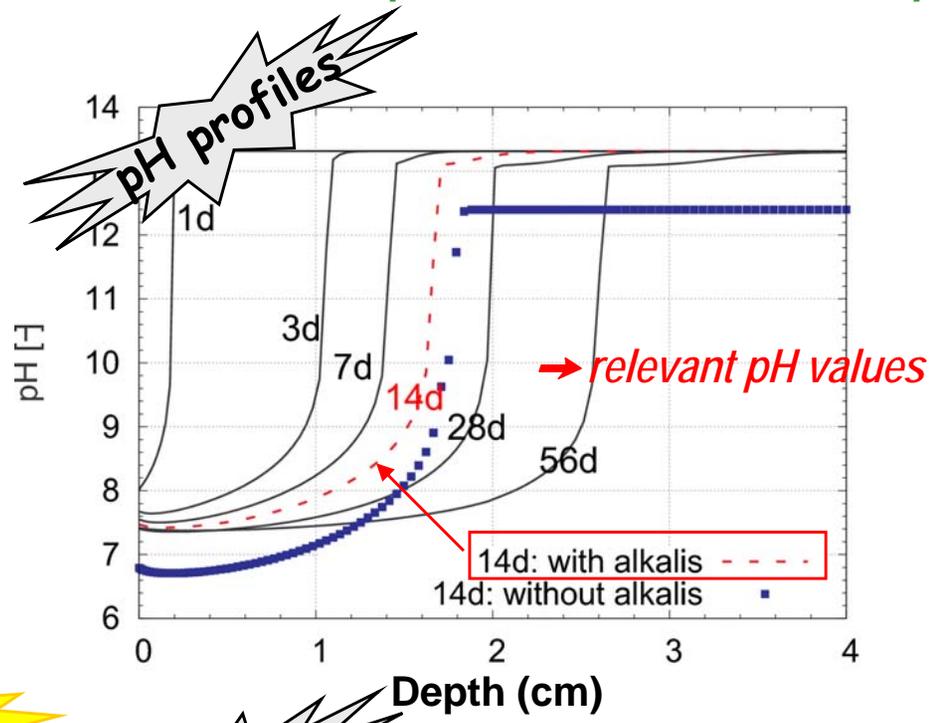
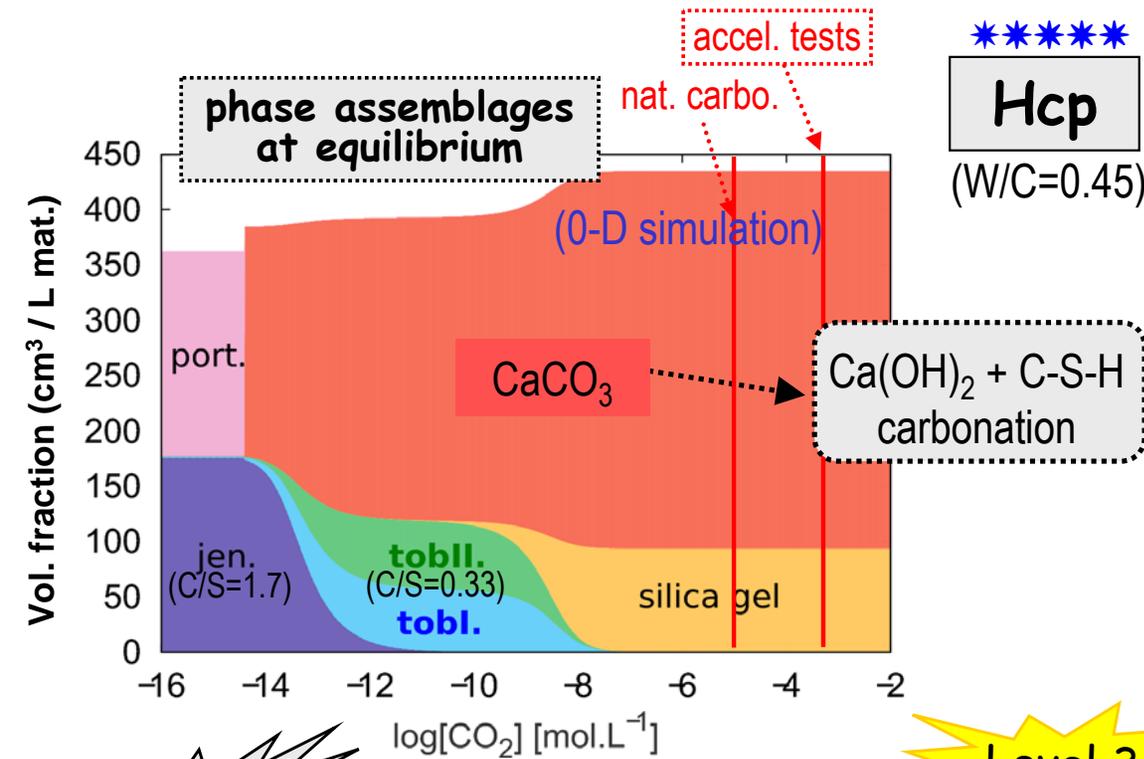
Physical

Chemical

Input data	value
$\phi_0$ (%)	42.0
$K_l^0$ ( $10^{-20}$ m <sup>2</sup> )	2
$S_{0l}$ (-)	RH = 53%
$p_c = p_c(S_l)$	exp. WVDI
$n_{CH}^0$ (mol.L <sup>-1</sup> )	5.6
$n_{C-S-H}^0$ (mol.L <sup>-1</sup> )	2.4
$[Na^+]$ (mol.L <sup>-1</sup> )	0.12
$[K^+]$ (mol.L <sup>-1</sup> )	0.24
$R_0$ ( $\mu$ m)	30

# 3.2 - NUMERICAL PHYSICAL-CHEMICAL MODEL: EXAMPLES OF SIMULATION

[Morandeau et al., CONMOD, 2010]



→ detailed & accurate predictions



# Outline

- 1 - Introduction
- 2 - Modelling of isothermal **Cl<sup>-</sup> transport** in concrete
  - 2.1 - Level 2: Multi-species transport model (sat. cond.)
  - 2.2 - Level 3: Advanced physical-chemical model (sat. cond.)
  - 2.3 - Level 4: Coupled moisture-ion transport model
- 3 - Modelling of **carbonation** of concrete
  - 3.1 - Level 2: Semi-analytical physical-chemical model - Probabilistic framework
  - 3.2 - Level 3: Numerical physical-chemical model
-  4 - ***Concluding remarks & further needed developments***



# 4 - CONCLUDING REMARKS

\*\*\*\*\*



flexibility

## \* Multi-level platform of numerical models for durability

- ↳ intended for different issues
- ↳ selection according to accuracy required, target lifetime, available data, ...

Engineering approaches

### • Intermediate levels

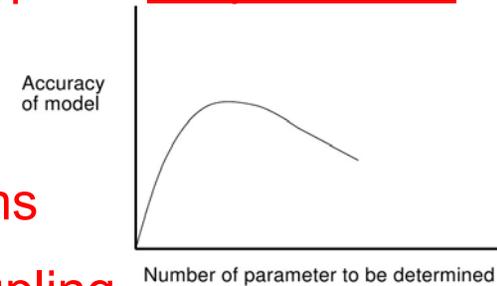
- ↳ num. inverse analysis (→ input data  $K_I$ ,  $D$ ,  $\mu$ ,  $\gamma$ )
- ↳ probabilistic approaches (→ account for uncertainties)
- ↳ [Cl<sup>-</sup>] profile / carbonation depth & SL prediction

↳ compromise between refinement & application  
(sufficient accuracy for various practical cases)

Advanced models

### • High levels

- ↳ validation of assumptions/mechanisms
- ↳ integration of transport-chemistry coupling
- ↳ integration of coupling between moisture & ionic/gaseous transports



### • Integrated **exp./num.** and performance-based approach

input      validation



# 4 - FURTHER DEVELOPMENTS NEEDED / OTHER APPROACHES



\*\*\*\*\*

... in order to improve the prediction of long-term durability

[Biernacki et al., ACI, 2001], [Buffo-Lacarrière et al., CCR, 2007], [Kolani, PhD, 2012]

- 1 - Further **coupling** with hydration models → account for early-age characteristics in field cond. ("covercrete")  
[Zhang et al., Microdurability, 2012]
- 2 - Better account for **hysteresis** effects (scanning curves) on **moisture transport**  
[Johannesson & Janz, B&E, 2009]  
[Zhang et al., SSCS 2012]
- 3 - Better description of **nano/microstructure** & its evolution  
[Bentz, 1997], [Ye, PhD, 2003], [Bishnoi & Scrivener, CCR, 2009]
- 4 - Account for impact of **cracking** on transport processes
- 5 - Advanced physical-chemical models → **Probabilistic** framework?  
↳ appropriate data bases !
- 6 - Further physical-chemical **coupling** or coupling with mechanics  
→ e.g. coupled moisture-ions-CO<sub>2</sub> transport model  
→ chemo-thermo-hygro-mechanical models → e.g. sulfate attack, frost action with deicing salts  
[Schrefler, SSCS, 2012]
- 7 - Integration of part of **propagation** period (corrosion, cracking, ...)  
[Alexander, Microdurability, 2012], [Michel et al. Microdurability, 2012]
- 8 - Enhanced **multi-scale** approach (nano→micro→macro ; material→**structure** ; 1D→2D→3D)  
→ e.g. 3-D integrated micro-material-structural modelling platform DuCOM-COM3  
e.g. [Maekawa & Ishida, 2001→2012]

SCMs

realistic SLD

engineering applications



Thank you for your attention ...

